

H0LiCOW V. New COSMOGRAIL time delays of HE 0435–1223: H_0 to 3.8% precision from strong lensing in a flat Λ CDM model

V. Bonvin,^{1*} F. Courbin,¹ S. H. Suyu,^{2,3} P. J. Marshall,⁴ C. E. Rusu,⁵ D. Sluse,⁶ M. Tewes,⁷ K. C. Wong,^{8,3} T. Collett,⁹ C. D. Fassnacht,⁶ T. Treu,¹⁰ M. W. Auger,¹¹ S. Hilbert,^{12,13} L. V. E. Koopmans,¹⁴ G. Meylan,¹ N. Rumbaugh,¹⁰ A. Sonnenfeld,^{15,10,16} and C. Spiniello²

¹Laboratoire d'Astrophysique, Ecole Polytechnique Fédérale de Lausanne (EPFL), Observatoire de Sauverny, CH-1290 Versoix, Switzerland

²Max Planck Institute for Astrophysics, Karl-Schwarzschild-Strasse 1, D-85740 Garching, Germany

³Institute of Astronomy and Astrophysics, Academia Sinica, P.O. Box 23-141, Taipei 10617, Taiwan

⁴Kavli Institute for Particle Astrophysics and Cosmology, Stanford University, 452 Lomita Mall, Stanford, CA 94035, USA

⁵Department of Physics, University of California, Davis, CA 95616, USA

⁶STAR Institute, Quartier Agora - Allée du six Août, 19c B-4000 Liège, Belgium

⁷Argelander-Institut für Astronomie, Auf dem Hügel 71, D-53121 Bonn, Germany

⁸National Astronomical Observatory of Japan, 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan

⁹Institute of Cosmology and Gravitation, University of Portsmouth, Burnaby Rd, Portsmouth PO1 3FX, UK

¹⁰Department of Physics and Astronomy, University of California, Los Angeles, CA 90095, USA

¹¹Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK

¹²Ezzellenzcluster Universe, Boltzmannstr. 2, 85748 Garching, Germany

¹³Ludwig-Maximilians-Universität, Universitäts-Sternwarte, Scheinerstr. 1, 81679 München, Germany

¹⁴Kapteyn Astronomical Institute, University of Groningen, P.O. Box 800, 9700-AV Groningen, The Netherlands

¹⁵Kavli IPMU (WPI), UTIAS, The University of Tokyo, Kashiwa, Chiba 277-8583, Japan

¹⁶Physics Department, University of California, Santa Barbara, CA, 93106, USA

Accepted XXX. Received YYY; in original form ZZZ

ABSTRACT

We present a new measurement of the Hubble Constant H_0 and other cosmological parameters based on the joint analysis of three multiply-imaged quasar systems with measured gravitational time delays. First, we measure the time delay of HE 0435–1223 from 13-year light curves obtained as part of the COSMOGRAIL project. Companion papers detail the modeling of the main deflectors and line of sight effects, and how these data are combined to determine the time-delay distance of HE 0435–1223. Crucially, the measurements are carried out blindly with respect to cosmological parameters in order to avoid confirmation bias. We then combine the time-delay distance of HE 0435–1223 with previous measurements from systems B1608+656 and RXJ1131–1231 to create a Time Delay Strong Lensing probe (TDSL). In flat Λ CDM with free matter and energy density, we find $H_0 = 71.9_{-3.0}^{+2.4}$ km s⁻¹ Mpc⁻¹ and $\Omega_\Lambda = 0.62_{-0.35}^{+0.24}$. This measurement is completely independent of, and in agreement with, the local distance ladder measurements of H_0 . We explore more general cosmological models combining TDSL with other probes, illustrating its power to break degeneracies inherent to other methods. The joint constraints from TDSL and Planck are $H_0 = 69.2_{-2.2}^{+1.4}$ km s⁻¹ Mpc⁻¹, $\Omega_\Lambda = 0.70_{-0.01}^{+0.01}$ and $\Omega_k = 0.003_{-0.006}^{+0.004}$ in open Λ CDM and $H_0 = 79.0_{-4.2}^{+4.4}$ km s⁻¹ Mpc⁻¹, $\Omega_{de} = 0.77_{-0.03}^{+0.02}$ and $w = -1.38_{-0.16}^{+0.14}$ in flat w CDM. In combination with Planck and Baryon Acoustic Oscillation data, when relaxing the constraints on the numbers of relativistic species we find $N_{\text{eff}} = 3.34_{-0.21}^{+0.21}$ in $N_{\text{eff}}\Lambda$ CDM and when relaxing the total mass of neutrinos we find $\Sigma m_\nu \leq 0.182$ eV in $m_\nu\Lambda$ CDM. Finally, in an open w CDM in combination with Planck and CMB lensing we find $H_0 = 77.9_{-4.2}^{+5.0}$ km s⁻¹ Mpc⁻¹, $\Omega_{de} = 0.77_{-0.03}^{+0.03}$, $\Omega_k = -0.003_{-0.004}^{+0.004}$ and $w = -1.37_{-0.23}^{+0.18}$.

Key words: cosmology: observations – distance scale – galaxies: individual (HE 0435–1223) – gravitational lensing: strong

1 INTRODUCTION

In the past decade, the Standard Cosmological Model, Λ CDM, which assumes the existence of either a cosmological constant or a form of dark energy with equation of state $w = -1$, and large scale structure predominantly composed of Cold Dark Matter, has been firmly established given observations to date (e.g. [Hinshaw et al. 2013](#); [Planck Collaboration et al. 2015a](#)). From a minimal set of 6 parameters describing Λ CDM, one can in principle infer the value of other parameters such as the current expansion rate of the Universe, H_0 . However, such an inference involves strong assumptions about the cosmological model, such as the absence of curvature or a constant equation of state for the dark energy. Conversely, we can relax these assumptions and explore models beyond flat- Λ CDM using a wider set of cosmological probes. In this case, the analysis benefits greatly from independent measurements of H_0 from observations of distance probes such as the distance ladder or water masers (see e.g. [Treu 2010](#); [Weinberg et al. 2013](#); [Treu & Marshall 2016](#), for a review). As [Weinberg et al. \(2013\)](#) point out, the Figure of Merit of any stage III or stage IV cosmological survey improves by 40% if an independent measurement of H_0 is available to a precision of 1%.

The “time-delay distances” in gravitationally lensed quasar systems offer an opportunity to measure H_0 independently of any other cosmological probe. First suggested by [Refsdal \(1964\)](#), this approach involves measuring the time delays between multiple images of a distant source produced by a foreground lensing object. The time delays depend on the matter distribution in the lens (galaxy), on the overall matter distribution along the line-of-sight and on the cosmological parameters. The time delays are related to the so-called time-delay distance $D_{\Delta t}$ to the lens and the source, which is primarily sensitive to H_0 and has a weak dependence on the matter density Ω_m , the dark energy density Ω_{de} , the dark energy equation of state, w , and on the curvature parameter Ω_k (e.g. [Linder 2011](#); [Suyu et al. 2010](#)).

The first critical step for the method to work is the measurement of the time delays from a photometric monitoring campaign to measure the shift in time between the light curves of the lensed images of quasars. Such monitoring campaigns must be long enough, and have good enough temporal sampling, to catch all possible (and usually small) photometric variations in the light curves. This is the goal of the COSMOGRAIL collaboration: the COSmological MONitoring of GRAvitational Lenses, which has been monitoring about 20 lensed quasars with 1m-class and 2m-class telescopes since 2004 (e.g. [Courbin et al. 2005](#); [Eigenbrod et al. 2006a](#); [Bonvin et al. 2016](#)). The target precision for the time delay measurements is a few percent or better, because the error on the time delays propagates linearly to first order on the cosmological distance measurement. Examples of COSMOGRAIL results include [Courbin et al. \(2011\)](#), [Tewes et al. \(2013b\)](#), [Rathna Kumar et al. \(2013\)](#), and [Eulaers et al. \(2013\)](#).

The second critical step is the modeling of the lens galaxy. Indeed, time-delay measurements alone can constrain only a combination of the time-delay distance and the surface density of the lens around the quasar images ([Kochanek 2002](#)). Additional constraints on the density profile of the lens are therefore required in order to convert ob-

served time delays into inferences of the time-delay distance. These constraints can be derived from velocity dispersion measurements, and the radial magnification of the extended, lensed arc image of the quasar host galaxy (e.g. [Suyu et al. 2010, 2014](#)). Ideal targets for this purpose are lensed quasars with a prominent host, which offer strong constraints on the density profile slope of the foreground lens.

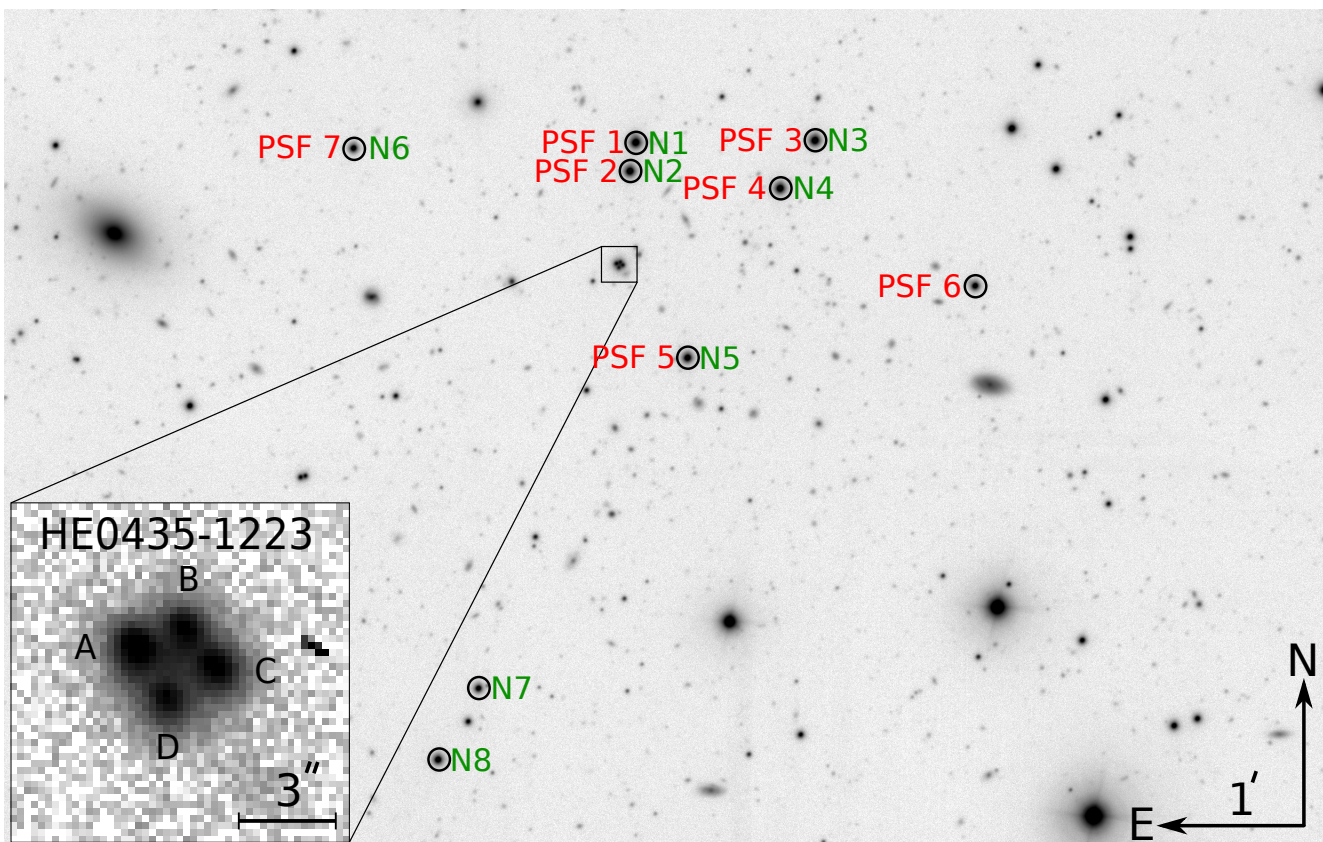
In modeling the lens mass distribution, special care has to be paid to the mass-sheet degeneracy (MSD), and, more generally, the source-position transformation (SPT) (e.g. [Falco et al. 1985](#); [Wucknitz 2002](#); [Schneider & Sluse 2013, 2014](#); [Xu et al. 2016](#); [Unruh et al. 2016](#)). These can be seen as degeneracies in the choice of the gravitational lensing potential that leave all the lensing observables invariant except for the modeled time delay, Δt . In other words, a wrong model of the main lens mass distribution can perfectly fit the observed morphology the lensing system, and yet result in an inaccurate inference of the time-delay distance. Priors and spectroscopic constraints on the dynamics of the main lens therefore play a critical role in avoiding systematic biases. In addition, perturbations to the lens potential by the distribution of mass along the line-of-sight also create degeneracies in the lens modeling. The latter can be mitigated with a measurement of the mass distribution along the line-of-sight, for example by using spectroscopic redshift measurements of the galaxies in the lens environment (e.g. [Fassnacht et al. 2006](#); [Wong et al. 2011](#)), comparisons between galaxy number counts in the real data and in simulations ([Hilbert et al. 2007, 2009](#); [Fassnacht et al. 2011](#); [Collett et al. 2013](#); [Greene et al. 2013](#); [Suyu et al. 2013](#); [McCully et al. 2016](#)) or using weak-lensing measurements ([Tihhonova et al.](#), in prep.)

The H0LiCOW collaboration (H_0 Lenses in COSMOGRAIL’s Wellspring) capitalizes on the efforts of COSMOGRAIL to measure accurate time delays, and on high quality auxiliary data from *Hubble Space Telescope* (*HST*) and 10-m class ground-based telescopes, to constrain cosmology. The H0LiCOW sample consists of five well-selected targets, each with exquisite time-delay measurements. B1608+656, monitored in radio band with the VLA ([Fassnacht et al. 2002](#)), and RXJ1131–1231, monitored by COSMOGRAIL in the visible ([Tewes et al. 2013b](#)), have already shown promising results, with relative precisions on the time-delay distance of 5% and 6.6% respectively ([Suyu et al. 2010, 2014](#)).

This paper is part of the H0LiCOW series, focusing on the quadruple lensed quasar HE 0435–1223 ($\alpha(2000)$: 04h 38m 14.9s; $\delta(2000)$: $-12^\circ 17' 14''.4$) ([Wisotzki et al. 2000, 2002](#)) discovered during the Hamburg/ESO Survey (HES) for bright quasars in the Southern Hemisphere. The source redshift has been measured by [Sluse et al. \(2012\)](#) as $z_s = 1.693$, and the redshift of the lens has been measured by [Morgan et al. \(2005\)](#) and [Eigenbrod et al. \(2006b\)](#) as $z_d = 0.4546 \pm 0.0002$. The lens lies in a group of galaxies of at least 12 members. A first measurement of the time delay for HE 0435–1223 was presented in [Courbin et al. \(2011\)](#). In this work, we present a significant improvement of the time delay measurement, with twice as long light curves as in [Courbin et al. \(2011\)](#). The other H0LiCOW papers include an overview of the project ([Suyu et al.](#), submitted; hereafter H0LiCOW Paper I), a spectroscopic survey of the field of HE 0435–1223 and a characterization of the groups along the line-of-sight ([Sluse et al.](#), submitted; here-

Table 1. Optical monitoring campaigns of HE0435–1223. The sampling is the mean number of days between the observations, not considering the seasonal gaps.

Telescope	Camera	FoV	Pixel	Period of observation	#obs	Exp.time	median FWHM	Sampling
Euler	C2	11'×11'	0.344"	Jan 2004 - Mar 2010	301	5×360s	1.37"	6 days
Euler	ECAM	14.2'×14.2'	0.215"	Sep 2010 - Mar 2016	301	5×360s	1.39"	4 days
Mercator	MEROPE	6.5'×6.5'	0.190"	Sep 2004 - Dec 2008	104	5×360s	1.59"	11 days
Maidanak	SITE	8.9'×3.5'	0.266"	Oct 2004 - Jul 2006	26	10×180s	1.31"	16 days
Maidanak	SI	18.1'×18.1'	0.266"	Aug 2006 - Jan 2007	8	6×300s	1.31"	16 days
SMARTS	ANDICAM	10'×10'	0.300"	Aug 2003 - Apr 2005	136	3×300s	≤1.80"	4 days
TOTAL	-	-	-	Aug 2003 - Mar 2016	876	394.5h	-	3.6 days

**Figure 1.** Part of the field of view of EulerCAM installed on the Swiss 1.2m telescope around the quasar HE0435–1223. This image is a combination of 100 exposures of 360s each, for a total exposure time of 10 hours. The stars used to build a PSF model for each EulerCAM exposure are circled and labeled PSF1 to PSF7 in red, and the stars used for the photometric calibrations are circled and labeled N1 to N8 in green. The insert in the bottom left shows the single, 360s exposure of the lens, for reference. Note that photometric and spectroscopic redshifts are available for many galaxies in the field of view (see H0LiCOW Paper II and H0LiCOW Paper III for details).

after H0LiCOW Paper II), a photometric survey of the field of HE0435–1223 with an estimate of the effect of the external line-of-sight structure (Rusu et al., submitted; hereafter H0LiCOW Paper III), and a detailed modeling of the lens and the inference of the time-delay distance along with cosmological results for HE0435–1223 (Wong et al., submitted; hereafter H0LiCOW Paper IV). In the present paper we combine the results for HE0435–1223 with those from the other two lensed quasars already published, and with other cosmological datasets (Bennett et al. 2013; Hinshaw et al. 2013; Planck Collaboration et al. 2015a).

This paper is organized as follows. Section 2 presents the COSMOGRAIL optical monitoring data and its reduction process. Section 3 presents the time-delay measurements and related uncertainties. Section 4 summarizes the main steps of the field-of-view analysis detailed in H0LiCOW Paper II and H0LiCOW Paper III and the lens modeling detailed in H0LiCOW Paper IV that lead to the time-delay distance determination. Section 5 combines the time-delay distance of HE0435–1223 and other lenses, and with additional cosmological datasets, in order to make the best possible inferences

of cosmological parameters. Finally, Section 6 presents our conclusions and future prospects in the light of these results.

2 PHOTOMETRIC MONITORING DATA

HE 0435–1223 has been monitored since 2003 as part of the COSMOGRAIL program and in collaboration with the Kochanek et al. (2006) team. The data acquired from autumn 2003 to spring 2010 were presented in Courbin et al. (2011). Here, we double the monitoring period, adding observations taken between autumn 2010 and spring 2016. Our monitoring sites include two Northern telescopes: the 1.2m Belgian Mercator telescope located at the Roque de Los Muchachos Observatory, La Palma, Canary Islands (Spain) and the 1.5m telescope located at the Maidanak Observatory (Uzbekistan). The average observing cadence was 11 and 16 days respectively at these sites. These telescopes ceased taking data for COSMOGRAIL in December 2008. In the Southern hemisphere, the Swiss 1.2m Euler telescope located at the ESO La Silla observatory (Chile) has monitored HE 0435–1223 since 2004. Two cameras were used: the C2 and the EulerCAM instruments, with an average cadence of 6 days and 4 days respectively. We also make use of the data obtained at the 1.3m SMARTS ANDICAM camera at Cerro Tololo Inter-American Observatory. Note that we do not re-analyse the SMARTS data, but use directly the published photometric measurements (Kochanek et al. 2006). Table 1 gives a detailed summary of the observations.

2.1 Data reduction

The full data set consists of two distinct blocks that do not overlap in time and that we treat independently. The first block includes the Mercator, Maidanak and Euler-C2 data, to which we add the published SMARTS photometry. The detailed processing and the relative photometric calibration of these curves is presented in Section 2.2 of Courbin et al. (2011). The second block consists of the 301 new data points obtained with EulerCAM that we reduce with the pipeline described in Section 3 of Tewes et al. (2013b), whose main steps can be summarized as follows:

(i) Each image is corrected for bias and readout effects. We then apply a flat-field correction using a high signal-to-noise master sky-flat which we correct for a pattern generated by the shutter opening and closing times. A spatially variable sky background frame is then constructed using the SExtractor software (Bertin & Arnouts 1996) and we subtract it from the data frame. All the frames are aligned and analyzed to carry out the photometric measurements. Figure 1 presents a stack of the 100 EulerCAM images with a seeing smaller than 1.14 arcsec.

(ii) The photometric measurements of the four blended images of HE 0435–1223 are obtained using deconvolution photometry using the MCS deconvolution algorithm (Magain et al. 1998; Cantale et al. 2016). To do this, the Point Spread Function (PSF) is measured, for each exposure individually, using the seven stars labeled PSF1 to PSF7 on Figure 1. A simultaneous deconvolution of all the frames is then carried out, leading to a model composed of a deep image representing extended sources, and a catalog of point

sources with improved resolution and sampling. During the deconvolution process the data are decomposed into a sum of analytical point sources (the quasar images) and of a numerical pixel channel containing the image of the lensing galaxy and of any potential extended object.

(iii) We compute a multiplicative median normalization coefficient for each exposure, using several deconvolved reference stars. If possible at all, we use stars whose color are similar to that of the quasar. In the case of HE 0435–1223, we use 8 reference stars, labeled N1 to N8 in Figure 1. We then apply the normalization coefficient to the deconvolved images of the point sources. Their intensities are returned for every frame, hence leading to the light curves.

The upper panel of Figure 2 presents the 13-year-long COSMOGRAIL light curves of HE 0435–1223, including the data from Courbin et al. (2011) and our new data. The similarity between the 4 light curves is immediately noticeable. However, it can also be noted that they would not superpose perfectly when shifted in time and magnitude, due to “extrinsic variability” which is interpreted as being caused by microlensing by stars in the lensing galaxy (see e.g. Blackburne et al. 2014; Braibant et al. 2014). These extrinsic contributions are clearly seen here on timescales from a few weeks to several years, in the form of an evolution of the magnitude-separation between the light curves. They must be handled properly in order to measure time delays with high accuracy.

2.2 On the importance of long light curves

Given the limited photometric precision of the COSMOGRAIL images, long-term monitoring is crucial to the time delay measurement, for two main reasons. First, one needs to catch enough intrinsic photometric variations in the quasar light curves in order to identify common structures. In the present case, these can be found on average 2-3 times per observing season, with some seasons displaying more prominent structures than others. Inflexion points in the light curves are most precious to constrain the time delays. For example, dips and peaks with an amplitude of nearly half a magnitude can be observed in several seasons: 2004-2005, 2012-2013 and 2015-2016. Second, the extrinsic variability related to microlensing must be taken into account (e.g. by modeling and removing it) to avoid time-delay measurement biases. Any simple and well-constrainable model is likely not sufficient to capture all aspects of this extrinsic variability, and might result in residual biases. The availability of decade long light curves allows us to check for potentially significant biases by analysing subsets of the full data, and certainly to reduce residual ones.

3 TIME-DELAY MEASUREMENT

With the light curves in hand, the time delays can be measured using numerical techniques accounting for noisy photometry, irregular temporal sampling and seasonal monitoring gaps. These techniques must also account for the extrinsic variability in the quasar images, related to microlensing effects, to avoid systematic error on the time-delay measurements. Different techniques have been devised in the

literature to carry out this task, and the COSMOGRAIL collaboration has implemented its own approach and several algorithms (see [Tewes et al. 2013a](#), also for a summary of extrinsic variability causes). These techniques are publicly available as a python package named `PyCS`¹. They have been tested using realistic numerical simulations, and have been confronted with the data provided to the lensing community by the first Time-Delay Challenge (TDC1; see [Dobler et al. 2015](#); [Liao et al. 2015](#)). An in-depth analysis of their performance proved them to be both precise and accurate ([Bonvin et al. 2016](#)) under various observational conditions, and in particular for light curves mimicking the COSMOGRAIL data. Among the three point-estimation algorithms provided in the `PyCS` toolbox, we consider for the present work two algorithms based on very different principles:

(i) **The free-knot spline technique** models the light curves as a sum of intrinsic variations of the quasar, common to the four light curves, plus some extrinsic variability different in each of the four light curves. The algorithm simultaneously fits one continuous curve for the intrinsic variations, four less-flexible curves for the extrinsic variations, and time shifts between the four light curves. All curves are represented as *free-knot* splines (see e.g. [Molinari et al. 2004](#)), for which the knot locations are optimised at the same time as the spline coefficients and the time shifts.

(ii) **The regression difference technique** minimises the variability of the difference between Gaussian-process regressions performed on each light curve. This method has no explicitly parametrised model for extrinsic variability. Instead, it yields time-delay estimates which minimize apparent extrinsic variability on time scales comparable to that of the precious intrinsic variability features. We see the contrasting approaches of this technique and the free-knot splines as valuable to detect potential method-related biases, and will use the regression difference technique as a cross-check of our results in this paper.

The third original `PyCS` estimator, a dispersion technique that was inspired by [Pelt et al. \(1996\)](#) and used in the previous analysis of HE 0435–1223 ([Courbin et al. 2011](#)) has proven to be less accurate in several investigations of simulated data (see [Eulaers et al. 2013](#); [Rathna Kumar et al. 2013](#); [Tewes et al. 2013a,b](#)). For this reason, we do not consider it in the present work.

We stress that the uncertainty estimation for the time delays is at least as important as the above point estimators. It is carried out within `PyCS` by assessing the point-estimation performance on synthetic light curves. This approach attempts to capture significantly more than the formal uncertainty which could be derived from the photometric error bars, if one would assume that for instance the spline model described above is a sufficient description of the data.

3.1 Application to the data

To apply the free-knot spline and regression difference techniques provided by `PyCS` to our data, we closely follow the

procedure described in [Tewes et al. \(2013a\)](#), and summarized in the following.² A key ingredient of this approach is the careful generation of mock light curves which are used to fine-tune and assess the precision and bias of the point estimators. These simulations are fully synthetic, in the sense that they are drawn from models with known time delays (hereafter *true* time delays), and yet they closely mimic the quasar variability signal and the extrinsic variability from the observed data. The `PyCS` free-knot spline technique is used to create the generative models from which we draw these simulations. For this, we start by fitting an intrinsic spline with on average 10 knots per year and four extrinsic splines with 2 knots per year to the observations. These average knot densities are sufficiently high to fit all unambiguous patterns observed in the data, while still resulting in a negligible intrinsic variance, i.e., avoiding significant degeneracies between the time-delay estimates and the spline models. Such a free-knot spline fit is illustrated in the second panel of [Figure 2](#). Before drawing the synthetic mock curves by sampling from this model fit, the smooth extrinsic splines are locally augmented with fast correlated noise. This noise follows a power-law spectrum which is iteratively adjusted so that the scatter in the mock curves has similar statistical properties to the scatter measured in the observed data. We then draw 1000 mock datasets, with true time shifts uniformly distributed within ± 3 days around our best-fitting solution. This results in a range of ± 6 days for the true delays, largely covering all plausible situations for this lens system. It is important to use simulations with various true time delays to tune and/or verify the accuracy of the point estimators. Tests on simulations with only a single true time delay would not probe bias and precision reliably, especially as many time-delay estimators are prone to responding unsteadily to the true delay.

The third panel of [Figure 2](#) shows the observed residual light curves after subtraction of a free-knot spline fit, and the bottom panel depicts the coverage by the different telescopes and instruments. During the first 5 years of monitoring, 3 to 4 different telescopes were used, with a mean residual dispersion of all data points of $\sigma = 25$ mmag. During the last years (2011 to present) one telescope was used, with a mean residual dispersion of $\sigma = 15$ mmag. Besides unmodeled microlensing effects, part of this scatter comes from night-to-night and instrument-to-instrument calibration of the data. Long-term monitoring programs of gravitational lenses are a matter of balance between the gain in temporal sampling using multiple telescopes, and the losses in photometric precision due to combining data from different instruments. Future monitoring programs will need to account for this trade-off ([Courbin et al. 2016](#), in prep).

We run the free-knot spline fit and the regression difference technique (with a Matérn covariance function, an amplitude parameter of 2.0 mag, a scale of 250 days, and a smoothness degree $\nu = 1.5$) on the observed light curves as well as on the mocks (for details, see [Tewes et al. 2013a](#)). [Figure 3](#) presents our time-delay estimates along with their 1σ uncertainties, and compares them to the previous measurements by [Courbin et al. \(2011\)](#), for which the disper-

¹ `PyCS` can be obtained from <http://www.cosmograil.org>

² For the sake of reproducibility, the complete python code used to measure the delays is available at <http://www.cosmograil.org>

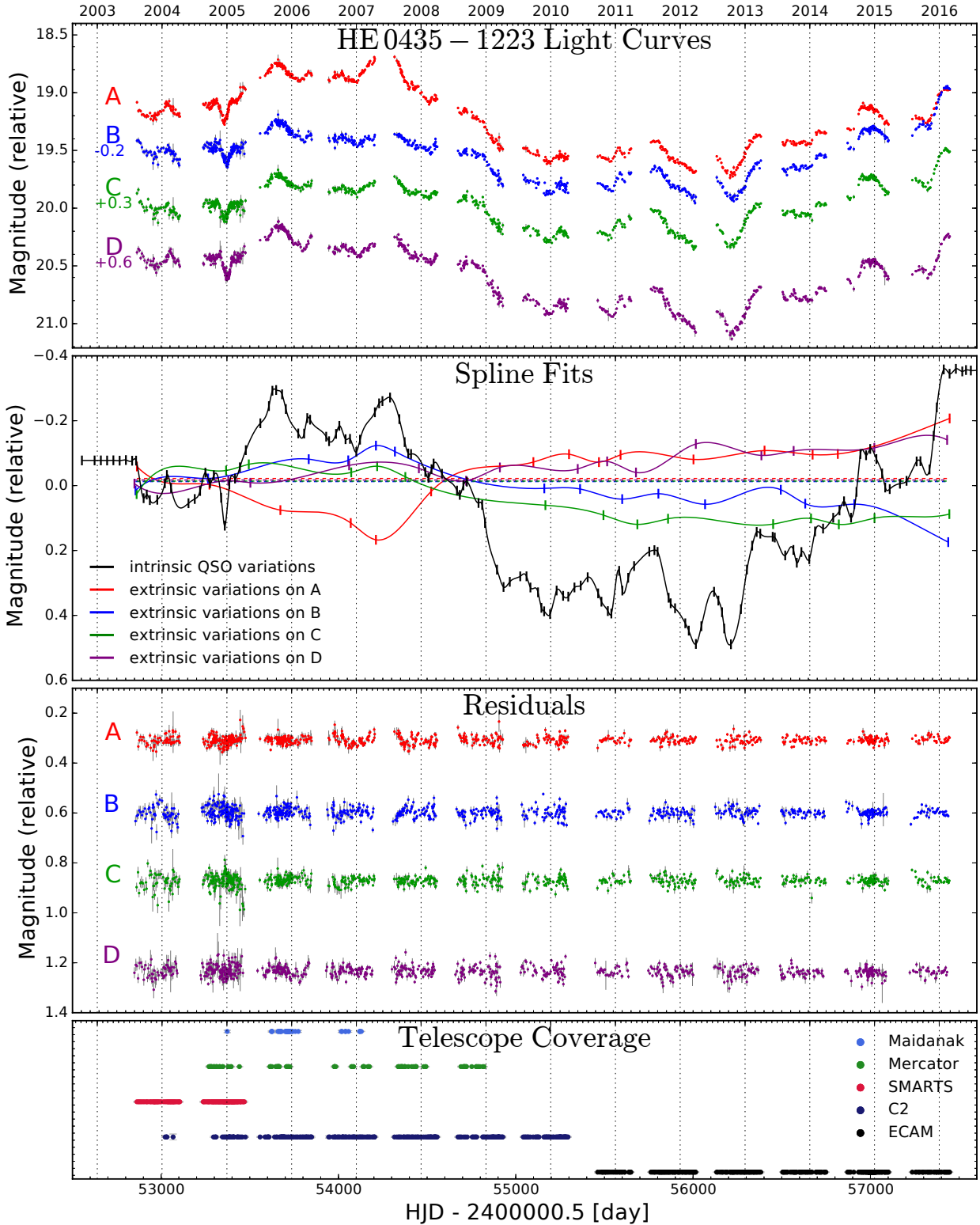


Figure 2. *From top to bottom:* Light curves for the four lensed images of the quasar HE 0435–1223. The relative shifts in magnitude are chosen to ease visualization, and do not influence the time-delay measurements. The second panel shows a model of the intrinsic variations of the quasar (black) and the 4 curves for the extrinsic variations in each quasar image using the free-knot spline technique (color code). The vertical ticks indicate the position of the spline knots. The residuals of the fits for each light curve is shown in the next panel. Finally, the bottom panel displays the journal of the observations for HE 0435–1223 for the 5 telescopes or cameras used to gather the data over 13 years (see column “#obs” of Table 1), where each point represents one monitoring night. The light curves will be made publicly available on the CDS and COSMOGRAIL websites once the paper is accepted for publication.

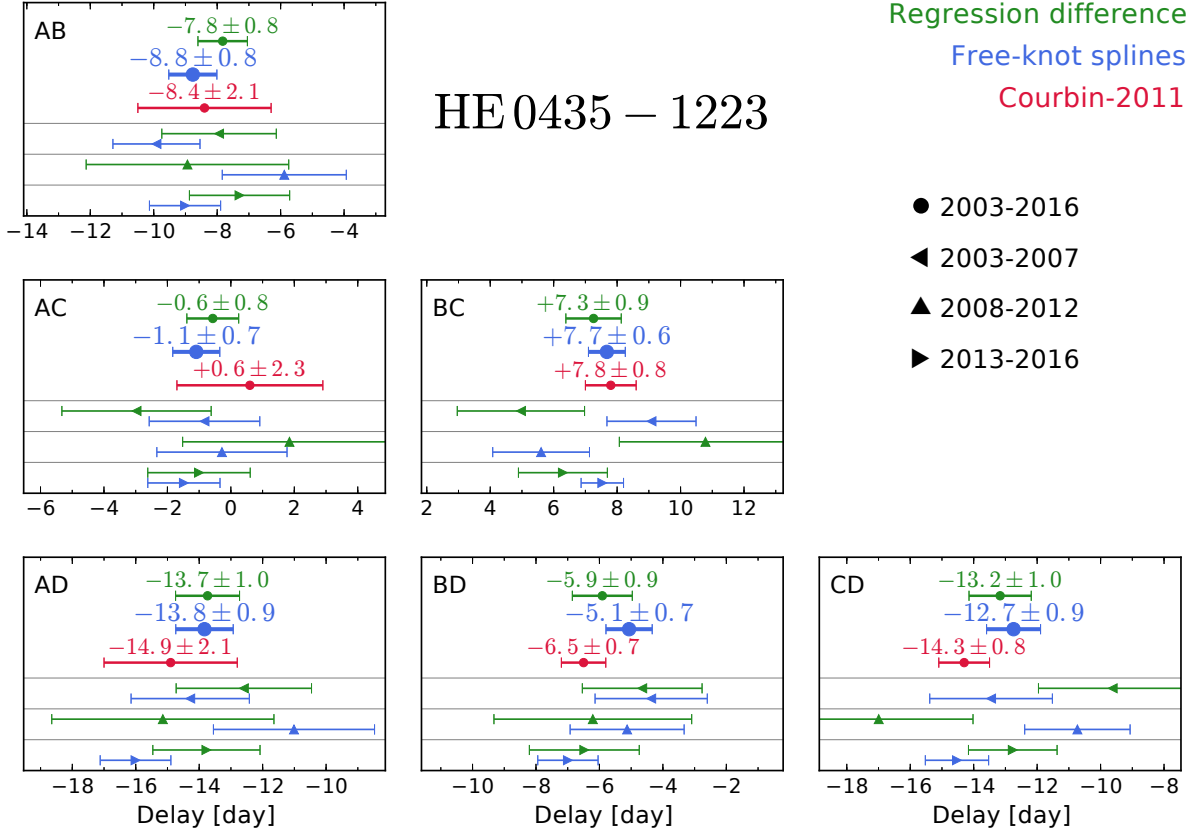


Figure 3. Time delays for the 6 pairs of quasar images, as indicated in top left corner of each panel. In each panel, we show the time delay measurement along with the 1σ error bar using our two best curve-shifting techniques, and we compare with the measurement of Courbin et al. (2011). We also show the result of measurements carried out with the free-knot spline technique and regression difference technique when splitting the data in 3 continuous chunks of 4 or 5 years each. All cosmological results in this work use the time delay measurements from the free-knot splines (larger blue symbols on the figure).

sion technique was used. The uncertainties are computed by summing the maximum estimated bias and statistical uncertainty in quadrature. The free-knot spline technique and regression difference technique are in relatively good agreement with each other, with a maximum tension of 1.3σ . Recall that the measurements are not independent, and therefore good agreement is to be expected. The two techniques also yield a similar precision, with a 6.5% relative uncertainty on the longest delay, i.e. Δt_{AD} .

3.2 Robustness checks

In order to test the robustness of our time-delay measurements, we performed several simple checks:

(i) We carried out several times the deconvolution of the ECAM data, using PSF stars and/or normalization stars that differ from the ones adopted in Figure 1. We also changed the initial parameters of the MCS deconvolution photometry. These include an estimate for the light profile of the lens galaxy, the astrometry of the quasar images and of lens galaxy and the flux of the quasar images at each epoch. All these changes resulted in a slightly higher scatter in the ECAM light curves data points, yet without significant impact on the time delay measurements.

(ii) We varied the intrinsic and/or extrinsic variability model of the free-knot spline technique by changing the number of knots used. We used 8 to 12 knots per year for the intrinsic model, and 0.5 to 2 knots per year for the extrinsic model. Free-knot splines have the advantage over regular splines or polynomials that their ability to fit prominent variability features is less sensitive to the total number of parameters. Using a lower or higher number of knots did not significantly affect the time-delay measurements. The residual light curves (third panel of Figure 2) remain statistically similar.

(iii) Taking advantage of the 13 years of monitoring, we split the light curves into three parts: i) seasons 2003-2004 to 2006-2007, ii) seasons 2007-2008 to 2011-2012 and iii) seasons 2012-2013 to 2015-2016. We measured the time delays independently on each of these subsections. The results are presented in the bottom parts of each panel of Figure 3. We see that the measurements on these subsections are well distributed around the delays measured on the full light curves. Furthermore, a clear majority of the delays obtained on the subsections cover, within the given 1σ error estimates, the results from the full curves. To conclude, these robustness checks give no strong evidence that the achieved time-delay uncertainties are significantly underestimated and/or biased.

3.3 Time delays of HE 0435–1223

We have shown that our two curve shifting techniques lead to comparable time delays and error bars on the full light curves of HE 0435–1223, which is reassuring. Still, one needs to define which time delay estimates to propagate into the time-delay distance (H0LiCOW Paper IV) and cosmological parameter inferences. We opt for using the results from the free-knot spline technique. This method has been tested extensively on a broad range of simulated light curves and proved to be both precise and accurate (Bonvin et al. 2016). In addition, Sluse & Tewes (2014) showed with this same technique that a flexible extrinsic variability model can prevent potential time delay biases due to the delayed emission of the Broad Line Region of the quasar with respect to the accretion disk.

4 TIME-DELAY DISTANCE

The time delays determined in Section 3, combined with a careful modeling of the lens galaxy mass distribution, can be used to infer the time-delay distance in the HE 0435–1223 system. The lens modeling and time-delay distance determination are addressed in detail in H0LiCOW Paper IV and are only summarized here.

4.1 Principles of the measurement

The time delay Δt_{ij} between two lensed images of the same object can be written as follows:

$$\Delta t_{ij} = \frac{D_{\Delta t}}{c} \left[\frac{(\theta_i - \beta)^2}{2} - \psi(\theta_i) - \frac{(\theta_j - \beta)^2}{2} + \psi(\theta_j) \right]. \quad (1)$$

where θ_i and θ_j are the coordinates of the images i and j in the lens plane, θ is the position of the lensed images on the plane of the sky, β is the unlensed source position and $\psi(\theta_i)$ is the lens potential at position θ_i . The time-delay distance $D_{\Delta t}$ is defined to be the following combination of three angular diameter distances and the deflector (i.e. the lens) redshift z_d : $D_{\Delta t} \equiv (1 + z_d)D_d D_s / D_{ds}$. Here, D_d , D_s and D_{ds} are respectively the angular distances between the observer and the deflector, the observer and the source, and the deflector and the source. The time-delay distance is, by construction, proportional to the inverse of the Hubble constant H_0^{-1} , and is primarily sensitive to this of all cosmological parameters. A posterior probability distribution for $D_{\Delta t}$ allows us to infer a probability distribution for H_0 , assuming a given cosmology.

In the case of HE 0435–1223, there are multiple galaxies at different redshifts close in projection to the strong lens system. We explicitly include these galaxies in our multi-plane lens model in H0LiCOW Paper IV, and in doing so introduce more angular diameter distances into the problem. However, we can still form the posterior predictive distribution for the “effective” time-delay distance defined above, and it is the latter that we use to infer cosmological parameters. All the remaining additional mass along the line-of-sight can also weakly focus and defocus the light rays from the source, an effect that needs to be corrected for.

We model this external contribution using an external convergence term κ_{ext} that modifies the time-delay distance as follows:

$$D_{\Delta t} = \frac{D_{\Delta t}^{\text{model}}}{1 - \kappa_{\text{ext}}}. \quad (2)$$

Here, $D_{\Delta t}^{\text{model}}$ is the effective time-delay distance predicted by the multi-plane model, and $D_{\Delta t}$ is the corrected time-delay distance we seek. Given probability density functions (PDFs) for $P(D_{\Delta t}^{\text{model}})$ and κ_{ext} , we can compute the PDF for $D_{\Delta t}$. In H0LiCOW Paper IV we derive a log-normal approximation for $P(D_{\Delta t})$, and it is this that we use as a likelihood function $P(D_{\Delta t}|\theta, H)$ for cosmological parameters θ given a cosmological model H .

In the rest of this section we provide a brief summary of each part of the analysis just outlined, before proceeding to the cosmological parameter inference in Section 5.

4.2 Determination of the external convergence

We use two complementary approaches to quantify the impact of the mass along the line-of-sight, both yielding consistent results.

4.2.1 Spectroscopy of the field

In H0LiCOW Paper II, we perform a spectroscopic identification of a large fraction of the brightest galaxies³ located within a projected distance of 3′ of the lens. This catalog is complemented with spectroscopic data from Momcheva et al. (2015) that augment redshift measurements to projected distances of ∼15′ from the lens. Based on those data, we show that, from the five galaxies located within 12 arcsec of the lens, the galaxy G1 ($z = 0.782$), closest in projection, produces the largest perturbation of the gravitational potential, and hence needs to be explicitly included in the lens models. The other galaxies are found to produce significantly smaller perturbations. On the other hand, we search for galaxy groups and clusters that would be massive enough to modify the structure of the lens potential, but find none. On the lower mass end (i.e. groups with $\sigma \leq 500 \text{ km s}^{-1}$), 9 group candidates are found in the vicinity of the lens. We demonstrate that none of the groups discovered is massive enough/close enough in projection to produce high order perturbation of the gravitational lens potential (McCully et al. 2014, 2016). This is also confirmed by a weak lensing analysis of the field of HE 0435–1223 (Tihhonova et al., in prep.)

4.2.2 Weighted galaxy number counts

In H0LiCOW Paper III, we calculate the probability distribution for the external convergence using a weighted galaxy number counts technique (Greene et al. 2013). We conduct

³ The completeness of the spectroscopic identification depends on the distance to the lens and limiting magnitude, see Figure 3 of H0LiCOW Paper II. For example, 60% (80%) of the galaxies brighter than $i \sim 22 \text{ mag}$ ($i \sim 21.5 \text{ mag}$) have a measured spectroscopic redshift within a radius of 3′ (2′) of the lens.

a wide-field, broad-band optical to mid-infrared photometric survey of the field in order to separate galaxies from stars, determine the spatial distribution of galaxies around HE 0435–1223, and estimate photometric redshifts and stellar masses. We compare weighted galaxy number counts around the lens, given an aperture and flux limit, to those through similar apertures and flux limits in CFHTLenS (Heymans et al. 2012). We investigate weights that incorporate the projected distance and redshift to the lens as well as the galaxy stellar masses. The resulting number under/overdensities serve as constraints in selecting similar fields from the Millennium Simulation, and their associated κ_{ext} values, from the catalog of Hilbert et al. (2009). We find that the resulting distribution of κ_{ext} is consistent with the typical mean density value (i.e. $\kappa_{\text{ext}}=0$) and is robust to choices of weights, apertures, flux limits and cosmology, up to an impact of 0.5% on the time-delay distance.

4.3 Mass modeling

In H0LiCOW Paper IV, we perform our lens modeling using GLEE, a software package developed by A. Halkola and S. H. Suyu (Suyu & Halkola 2010; Suyu et al. 2012). Our fiducial mass model for the lens galaxy is a singular power-law elliptical mass distribution with external shear. We explicitly include the closest line-of-sight perturbing galaxy in the lens model (G1; see Figure 3 of H0LiCOW Paper IV), using the full multiplane lens equation to account for its effects. We also include in an extended modeling four other nearby perturbing galaxies to check their impact. Because the perturbers are at different redshifts, there is no single time-delay distance that can be clearly defined. Instead, we vary H_0 directly in our models and then use this distribution to calculate an effective time-delay distance, where the angular diameter distances D_d and D_s are calculated using the redshift of the main deflector, $z_d = 0.454$. We assume a fiducial cosmology, $\Omega_m = 0.3$, $\Omega_\Lambda = 0.7$, and $w = -1$ in this modeling procedure, but we find that allowing these cosmological parameters to vary has a negligible ($< 1\%$) effect on the resulting effective time-delay distance distribution.

The mass sheet degeneracy—the invariance to the lensed images under addition of a uniform mass sheet to our mass model combined with a rescaling of the source plane coordinates—can affect the inferred time delays, and may limit the effectiveness of time delays in constraining cosmology (e.g. Schneider & Sluse 2013, 2014). We have shown in previous work that including the central velocity dispersion of the main galaxy in the lens modeling minimizes the effect of the mass sheet degeneracy (see Figure 4 of Suyu et al. 2014). In the case of HE 0435–1223 we measure $\sigma = 222 \pm 15 \text{ km s}^{-1}$ using Keck I spectroscopy. We also show that mass models that go beyond the elliptically-symmetric power-law profile, and that are better physically justified, fit our data equally well yet lead to the same cosmological inference. As in Suyu et al. (2014), the H0LiCOW Paper IV tests both power-law and a composite model with a baryonic component and a NFW dark matter halo. We also note that the completely independent models of Birrer et al. (2015) confirm the findings of Suyu et al. (2014).

We model the images of the lensed source simultaneously in three *HST* bands: ACS/F555W, ACS/814W, and WFC3/F160W. The lensed quasar images are modeled as

point sources convolved with the PSF. The extended, unlensed image of the host galaxy of the quasar is modeled separately on a pixel grid with curvature regularization (see e.g. Suyu et al. 2006). Our constraints on the model include the positions of the quasar images, the measured time delays, and the surface brightness pixels in each of the three bands. Model parameters of the lens are explored through Markov Chain Monte Carlo (MCMC) sampling, while the Gaussian posterior PDF for the source pixel values is characterized using standard linear algebra techniques (e.g. Suyu et al. 2006).

During our modeling procedure, we iteratively update the PSFs using the lensed AGN images themselves in a manner similar to Chen et al. (2016), and we use these corrected PSFs in our final models (for more details, see Suyu et al. in preparation). We account for various systematic uncertainties related to our choice of modeling regions, our assumed light profiles for the lens galaxy, the effects of additional line-of-sight perturbers and alternative mass models, and combine the resulting posterior PDFs for $D_{\Delta t}$ into a single distribution.

4.4 Blinding methodology and unblinded results

A key element of our analysis is that it is carried out blindly with respect to the inference of cosmological parameters. This blindness is crucial in order to avoid unconscious confirmation bias. In practice, blindness is built into our measurement in the following manner. All the individual measurements and modeling efforts in H0LiCOW Paper IV are carried out without any knowledge of the effects of specific choices on the resulting cosmology. In some cases, this blindness is trivial to achieve: for example the measurement of velocity dispersion was carried out and finalized independently from the cosmological inference, and the connection between the two is significantly complex and indirect that the person carrying out the velocity dispersion measurement effectively had no way to determine how that could affect cosmological parameters. In other cases, building on the procedure established by our previous analysis of RXJ1131–1231 (Suyu et al. 2013), blindness was achieved by only using plotting codes that offset every posterior probability distribution for time-delay distance and cosmological parameters by a constant (such as the median value of each marginal distribution), and thus never revealing the actual measurements to the investigators until the time of unblinding (see discussion in H0LiCOW Paper IV).

All of our analysis and visualization tools were developed and tested using simulated quantities. No modifications were allowed after the official unblinding, making the unblinding step irreversible. The official unblinding was originally scheduled for June 2 2016 during a teleconference open to all the co-authors. Additional tests were suggested during this meeting. As a result, the analysis was kept blind for another two weeks and the final unblinding happened during a teleconference starting at 6AM UT on June 16 2016 and was audio recorded by LVKE without others knowing until the end of the teleconference. The results presented in the next section are the combination of the blind measurements

obtained for HE0435–1223 and RXJ1131–1231⁴, and the not-blind measurements obtained by our team for the first system B1608+656.

5 JOINT COSMOGRAPHY ANALYSIS

CMB experiments provide a model-dependent value of the Hubble constant, H_0 , which appear to be in some tension with methods based on standard rulers and standard candles. In a flat Λ CDM universe, the significance of the tension between the most recent values from Planck (Planck Collaboration et al. 2015a) and the direct measurement from Cepheids and Type Ia Supernovae (Riess et al. 2016) is 3.3σ . Either this tension is due, at least in part, to systematics in the measurements (as suggested by e.g. Efstathiou 2014), or it is caused by new physics beyond the predictions of flat Λ CDM. Several authors discuss the possibility of relaxing the usual assumptions about cosmological parameters as a way to reduce the tension (e.g. Salvatelli et al. 2013; Heavens et al. 2014; Di Valentino et al. 2016). Possible assumptions include, for example, that we live in a non-flat universe ($\Omega_k \neq 0$), that the dark energy equation of state is not a cosmological constant ($w \neq -1$), that the sum of the neutrino masses is larger than predicted by the standard hierarchy scenario ($\Sigma m_\nu > 0.06$ eV), and/or that the effective number of relativistic neutrino species may differ from its assumed value in the standard model ($N_{\text{eff}} \neq 3.046$). Given the above, it is important to consider a range of plausible extended cosmological models when investigating the information that can be gained from any specific cosmological probe (see e.g. Collett & Auger 2014; Giusarma et al. 2016).

In this context, we present below our inference of the cosmological parameters obtained using the time-delay distance measurements of the strongly lensed quasars B1608+656, WFI2033–4723 and HE0435–1223. After making sure that their individual results are consistent with each other, we present our cosmological inference using all three systems jointly, referred as “TDSL” for “Time Delay Strong Lensing.” We then combine TDSL with the WMAP Data Release 9 (Bennett et al. 2013; Hinshaw et al. 2013, hereafter “WMAP”) and with the Planck 2015 Data Release⁵ (Planck Collaboration et al. 2015a, hereafter “Planck”). When available, we also use the combination of Planck data with Planck measurements of CMB weak-lensing (Planck Collaboration et al. 2015b, hereafter “CMBL”), with Baryon Acoustic Oscillations surveys at various redshifts (Percival et al. 2010; Beutler et al. 2011; Blake et al. 2011; Anderson et al. 2012; Padmanabhan et al. 2012, hereafter BAO) and with the data of the Joint Lightcurve Analysis of Supernovae (Betoule et al. 2013, hereafter “JLA”). The latter two datasets are described in detail in Section 5.2 of Planck Collaboration et al. (2014) and Section 5.3 of Planck Collaboration et al. (2015a) respectively. Note that when possible, we

⁴ The time-delay distance measurement of RXJ1131–1231 from Suyu et al. (2014) that includes a composite model for the lens was not blind, whereas the first measurement of this same lens from Suyu et al. (2013) was done blindly.

⁵ We use the Planck chains designated by “plikHM_LTT_lowTEB” that uses the baseline high-L Planck power spectra and low-L temperature and LFI polarization.

Table 2. Description of the cosmological models considered in this work. WMAP refers to the constraints given in the WMAP Data Release 9. Planck refers either to the constraints from Planck 2015 Data Release alone, or combined with CMBL, BAO and/or JLA. See Section 5 for details.

Model name	Description
UH_0	Flat Λ CDM cosmology $\Omega_m = 1 - \Omega_\Lambda = 0.32$ H_0 uniform in $[0, 150]$
U Λ CDM	Flat Λ CDM cosmology $\Omega_m = 1 - \Omega_\Lambda$ H_0 uniform in $[0, 150]$ Ω_m uniform in $[0, 1]$
U w CDM	Flat w CDM cosmology H_0 uniform in $[0, 150]$ Ω_{de} uniform in $[0, 1]$ w uniform in $[-2.5, 0.5]$
Uo Λ CDM	Non-flat Λ CDM cosmology $\Omega_m = 1 - \Omega_\Lambda - \Omega_k > 0$ H_0 uniform in $[0, 150]$ Ω_Λ uniform in $[0, 1]$ Ω_k uniform in $[-0.5, 0.5]$
o Λ CDM	Non-flat Λ CDM cosmology WMAP/Planck for $\{H_0, \Omega_\Lambda, \Omega_m\}$ $\Omega_k = 1 - \Omega_\Lambda - \Omega_m$
N_{eff} Λ CDM	Flat Λ CDM cosmology WMAP/Planck for $\{H_0, \Omega_\Lambda, N_{\text{eff}}\}$
m_ν Λ CDM	Flat Λ CDM cosmology WMAP/Planck for $\{H_0, \Omega_\Lambda, \Sigma m_\nu\}$
w CDM	Flat w CDM cosmology Planck for $\{H_0, w, \Omega_{\text{de}}\}$
$N_{\text{eff}}m_\nu$ Λ CDM	Flat Λ CDM cosmology Planck for $\{H_0, \Omega_\Lambda, \Sigma m_\nu, N_{\text{eff}}\}$
o w CDM	Open Λ CDM cosmology Planck for $\{H_0, \Omega_{\text{de}}, \Omega_k, w\}$

do not combine the cosmological probes other than TDSL ourselves, but instead we use the combined results published and provided by the Planck team⁶.

We follow the importance sampling approach suggested by Lewis & Bridle (2002) and employed by Suyu et al. (2010) and Suyu et al. (2013), re-weighting the WMAP and Planck posterior samples with the TDSL likelihoods from the analyses of B1608+656 (Suyu et al. 2010), RXJ1131–1231 (Suyu et al. 2014) and HE0435–1223 (HOLICOW Paper IV), for the set cosmological models described in Table 2.

We consider both i) “uniform” cosmologies, with only a few variable cosmological parameters with uniform priors in order to get constraints from TDSL alone, and ii) cosmologies extended beyond Λ CDM where we combine the TDSL likelihoods with other probes. When comparing two

⁶ <http://pla.esac.esa.int/pla/#cosmology>

Table 3. Parameters of the three strong lenses used in our analysis. μ_D, σ_D and λ_D are related to the analytical fit of the time-delay distance probability function (see Eq. 3).

Name	Reference	z_d	z_s	μ_D	σ_D	λ_D
B1608+656	Suyu et al. (2010)	0.6304	1.394	7.0531	0.22824	4000.0
RXJ1131–1231	Suyu et al. (2014)	0.295	0.654	6.4682	0.20560	1388.8
HE0435–1223	H0LiCOW Paper IV	0.4546	1.693	7.5793	0.10312	653.9

cosmological parameter inferences, we use the following terminology. When two results differ by less than 1σ we consider that they are “consistent;” in the $1-2\sigma$ range they are in “mild tension;” in the $2-3\sigma$ range they are in “tension;” above 3σ , they are in “significant tension.” If a cosmological parameter inference follows a non-Gaussian distribution, we use “ 1σ ” to refer to the width of the distribution between its 50th and 16th percentiles if the comparison is made towards a lower value, and between its 50th and 84th percentiles if the comparison is made towards a higher value. In a comparison, the σ values always refer to those belonging to the distribution that includes TDSL.

5.1 Cosmological inference from Strong Lensing alone

We first present our values for the cosmological parameters that can be inferred from TDSL alone. We use the time-delay distance likelihoods analytically expressed with a skewed log-normal distribution:

$$P(D_{\Delta t}) = \frac{1}{\sqrt{2\pi}(x - \lambda_D)\sigma_D} \exp\left[-\frac{(\ln(x - \lambda_D) - \mu_D)^2}{2\sigma_D^2}\right], \quad (3)$$

where $x = D_{\Delta t}/(1 \text{ Mpc})$. We recall in Table 3 the lens and source redshifts of the three strong lenses as well as the parameters μ_D, σ_D and λ_D describing their respective time-delay distance distributions.

5.1.1 Combination of three lenses

Before carrying out a joint analysis of our three lens systems, we first perform a quantitative check that our three lenses can be combined without any loss of consistency. For that purpose, we compare their time-delay distance likelihood functions in the full cosmological parameter space, and measure the degree to which they overlap. Following Marshall et al. (2006) and Suyu et al. (2013), we compute the Bayes factor F , or evidence ratio, in favor of a simultaneous fit of the lenses using a common set of cosmological parameters. When comparing three data sets $\mathbf{d}_1, \mathbf{d}_2$ and \mathbf{d}_3 , we can either assume the hypothesis H^{global} that they can be represented using a common global set of cosmological parameters, or the hypothesis H^{ind} that at least one data set is better represented using another independent set of cosmological parameters. We stress that this latter model would make sense if there was a systematic error present that led to a vector offset in the inferred cosmological parameters. To parametrize this offset vector with no additional information would take as many nuisance parameters as there are dimensions in the cosmological parameter space; assigning

uninformative uniform prior PDFs to each of the offset components is equivalent to using a complete set of independent cosmological parameters for the outlier 5 dataset.

The Bayes factor, that makes the H^{global} hypothesis F times more probable than H^{ind} can be computed as follows:

$$F = \frac{P(\mathbf{d}_1, \mathbf{d}_2, \mathbf{d}_3 | H^{\text{global}})}{P(\mathbf{d}_1 | H^{\text{ind}})P(\mathbf{d}_2 | H^{\text{ind}})P(\mathbf{d}_3 | H^{\text{ind}})}. \quad (4)$$

A Bayes factor F significantly larger than 1 indicates that the considered data sets can be consistently combined. In the present case, considering three lenses with known time-delay distance likelihoods $\mathbf{L}_1, \mathbf{L}_2$ and \mathbf{L}_3 , the Bayes factor becomes:

$$F_{1 \cup 2 \cup 3} = \frac{\langle \mathbf{L}_1 \mathbf{L}_2 \mathbf{L}_3 \rangle}{\langle \mathbf{L}_1 \rangle \langle \mathbf{L}_2 \rangle \langle \mathbf{L}_3 \rangle}, \quad (5)$$

where angle brackets denote averages over our ensembles of prior samples. We can also compare the likelihoods pair by pair (1-versus-1) as in Equation 27 of Suyu et al. (2013) and then combine each pair with the third likelihood (2-versus-1):

$$F_{12 \cup 3} = \frac{\langle \mathbf{L}_1 \mathbf{L}_2 \mathbf{L}_3 \rangle}{\langle \mathbf{L}_1 \mathbf{L}_2 \rangle \langle \mathbf{L}_3 \rangle}. \quad (6)$$

This last equation allows us to check that the lenses can also be well combined pair-wise, and that none of them is inconsistent with the two others considered together. We compute the Bayes Factors $F_{1 \cup 2 \cup 3}$ and all the possible 1-versus-1 and 2-versus-1 permutations in the uniform cosmologies $UH_0, U\Lambda\text{CDM}, Uw\text{CDM}$, and $Uo\Lambda\text{CDM}$. We find that all the combinations are in good agreement, the only exception being for the pair $B1608+656 \cup RXJ1131-1231$, which is only marginally consistent in the $Uo\Lambda\text{CDM}$ cosmology ($F_{1 \cup 2}=1.1$). Considering the likelihoods individually, the three lenses are in excellent agreement, with a Bayes Factor $F_{1 \cup 2 \cup 3} = 21.3$ in UH_0 , $F_{1 \cup 2 \cup 3} = 14.2$ in $U\Lambda\text{CDM}$, $F_{1 \cup 2 \cup 3} = 18.9$ in $Uw\text{CDM}$ and $F_{1 \cup 2 \cup 3} = 10.8$ in $Uo\Lambda\text{CDM}$. We conclude that the time delay likelihoods of our three lenses can be combined without any loss of consistency.

5.1.2 Constraints in uniform cosmologies

Figure 4 presents the marginalized posterior PDF for H_0 in the cosmological models using uniform priors. Our baseline model, UH_0 , has a uniform prior on H_0 in the range $[0, 150] \text{ km s}^{-1} \text{ Mpc}^{-1}$, a matter density fixed at $\Omega_m = 0.32$ from the most recent Planck results (Planck Collaboration et al. 2015a), zero curvature $\Omega_k = 0$ and consequently a fixed cosmological constant. This model has only one free parameter. From left to right in the figure, we present this UH_0 cosmology, and then three models that have two or three free parameters (H_0 plus one or two others): the $U\Lambda\text{CDM}$

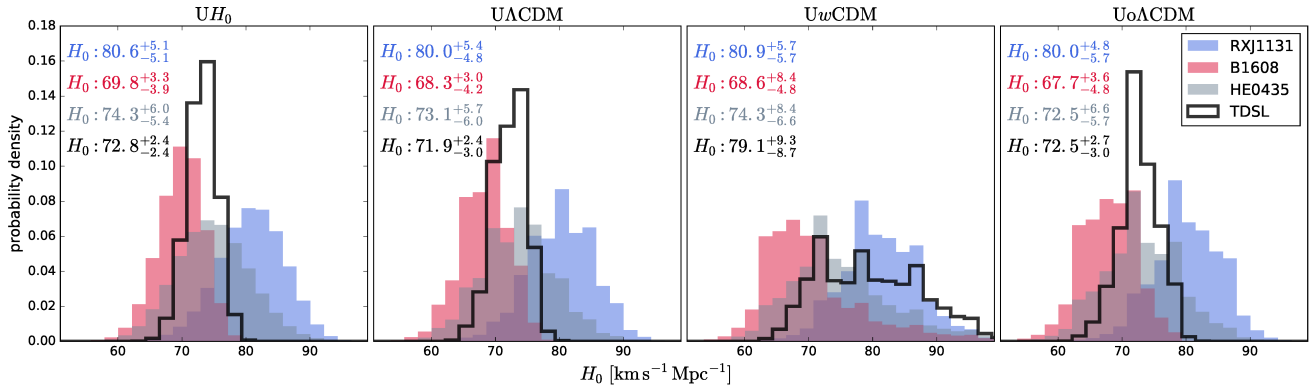


Figure 4. Marginalized posterior probability distributions for H_0 in the UH_0 , UACDM, $UwCDM$ and $Uo\Lambda$ CDM cosmologies using the constraints from the three strong lenses B1608+656, RXJ1131–1231 and HE0435–1223. The overlaid histograms present the distributions for each individual strong lens (ignoring the other two datasets), and the solid black line corresponds to the distribution resulting from the joint inference from all three datasets (TDSL). The quoted values of H_0 in the top-left corner of each panel are the median, 16th and 84th percentiles.

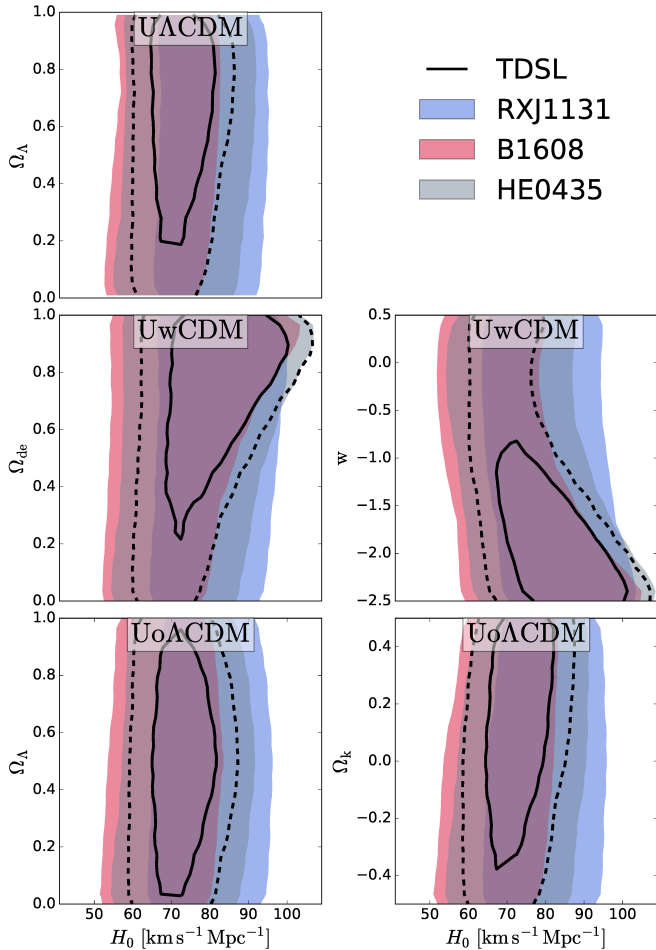


Figure 5. Comparison of the three strong lenses in the UACDM (top), $UwCDM$ (middle) and $Uo\Lambda$ CDM (bottom) cosmologies. The colored overlays delimit the 95% credible region for B1608+656, RXJ1131–1231 and HE0435–1223. The solid and dashed black lines draw the contours of the 68.3% and 95% credible regions, respectively, for the combination of the three lenses.

cosmology where we allow Ω_m to vary with uniform prior; the $UwCDM$ cosmology with a free Ω_{de} and a free time-independent dark energy equation of state w , both with uniform priors; and finally the $Uo\Lambda$ CDM cosmology, that relaxes the constraint on the curvature Ω_k and allows both this and Ω_Λ to vary with uniform priors. We quote in each panel the corresponding median and 1σ uncertainties of H_0 . In the UH_0 cosmology, combining the three lenses yields a value $H_0 = 72.8 \pm 2.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$, with 3.3% precision. When relaxing the constraint on Ω_m in UACDM (and thus being completely independent of any other measurement), we obtain $H_0 = 71.9^{+2.4}_{-3.0} \text{ km s}^{-1} \text{ Mpc}^{-1}$, with 3.8% precision. These two estimates are respectively 2.5σ and 1.7σ higher than the most recent Planck measurement in a flat- Λ CDM universe ($H_0 = 66.93 \pm 0.62 \text{ km s}^{-1} \text{ Mpc}^{-1}$; Planck Collaboration et al. 2015a), in excellent agreement with the most recent results using distance ladders ($H_0 = 73.00 \pm 1.75 \text{ km s}^{-1} \text{ Mpc}^{-1}$; Riess et al. 2016), and compatible with other local estimates (see e.g. Bonamente et al. 2006; Freedman et al. 2012; Sorce et al. 2012; Gao et al. 2016). Whether the tension between the local and cosmological measurements of H_0 comes from systematic errors or hints at new physics beyond flat- Λ CDM is currently a hot topic of discussion in the community (see e.g. Efstathiou 2014; Planck Collaboration et al. 2015a; Rigault et al. 2015; Spergel et al. 2015; Addison et al. 2016; Di Valentino et al. 2016; Riess et al. 2016, and references therein).

Figure 5 presents the two-dimensional 95% credible regions of the cosmological parameters in the $UwCDM$, $Uo\Lambda$ CDM, and UACDM cosmologies for each lens individually and for their combination (TDSL). Time Delay Strong Lensing is primarily sensitive to H_0 , and the tilt in the $H_0 - \Omega_\Lambda$, $H_0 - w$, and $H_0 - \Omega_k$ planes illustrates its weak sensitivity to the dark energy density, dark energy equation of state and curvature density, respectively. TDSL alone agrees both with a flat universe and a cosmological constant, although on the latter the credible region extends deeply into the phantom dark energy domain ($w < -1$). In the $UwCDM$ cosmology the correlation between H_0 and w is more prominent than in the other models, leading to a larger dispersion of the H_0 distribution in the corresponding panel of Figure 4. This highlights the fact that our cosmological in-

ferences in this cosmology are more sensitive to the prior range we choose. Thus, the resulting parameter values must be considered as indicative of a trend rather than as absolute measurements. We summarize our values for H_0 , Ω_k , w and Ω_m from TDSL alone in the top section of Table 4.

5.2 Constraining cosmological models beyond Λ CDM

We now investigate how strong lensing can help constrain cosmological models beyond standard flat Λ CDM, when combined with other cosmological probes. We demonstrated in Section 5.1 and Figure 5 that TDSL is only weakly dependent on the matter density, the dark energy density, the dark energy equation of state and the curvature. However, the cosmological parameter degeneracies for TDSL are such that the combination of TDSL with other probes can rule out large areas of parameter space. Following the motivations presented in Planck Collaboration et al. (2015a) for extensions to the base Λ CDM model, we present in the following a selection of models where we combine TDSL with the results from WMAP, Planck, Planck+BAO, Planck+BAO+CMBL and Planck+BAO+JLA when available. Figures 6 and 7 present the results. Note that we have smoothed the contours of the credible regions after importance sampling due to the sparsity of the WMAP and Planck MCMC chains, checking that the 95% credible regions do indeed contain approximately 95% of the importance weight.

5.2.1 One-parameter extensions

We first consider one-parameter extensions to the standard model, where we relax the constraints on one additional cosmological parameter from flat Λ CDM. We present in Figure 6 the two-dimensional marginalized parameter space for a selection of cosmological models for which the impact of TDSL is the most meaningful.

In the $\text{o}\Lambda$ CDM model, we consider a non-flat Universe with $\Omega_k \neq 0$. In the $N_{\text{eff}}\Lambda$ CDM model, we consider a variable effective number of relativistic neutrino species N_{eff} with a fixed total mass of neutrinos $\Sigma m_\nu = 0.06$ eV. In the $m_\nu\Lambda$ CDM model we consider a variable Σm_ν with a fixed $N_{\text{eff}} = 3.046$. Finally, in the w CDM model we consider a time-invariant dark energy equation of state w . A detailed description of these models is given in Table 2.

For each probe, or combination of probes, we draw the 95% credible region contours as colored lines. When combined with TDSL, the updated credible region is displayed as a filled area. When importance sampling using priors based on other probes, it is important to verify that the respective constraints in the parameter space overlap. If they do not, the probes considered may not be efficiently combined. With this in mind, we plot in each cosmology the 95% credible region for TDSL only (and uniform priors) as thin solid black lines. We note that in all one-parameter extensions presented here, the 2D marginalized TDSL and Planck 95% credible regions at least partially overlap, although in the $\text{o}\Lambda$ CDM and $m_\nu\Lambda$ CDM cosmologies, the 1D marginalized posterior mean value for H_0 from TDSL lies outside the 95% credible region of Planck. We consider the overlaps to be sufficient to justify our importance sampling TDSL with

Planck, but emphasize that the joint constraints must be interpreted cautiously. WMAP and Planck constraints are in agreement with each other, this being at least partly due to the large parameter space covered in the credible region of WMAP. This also results in a much wider overlap with the TDSL 95% credible regions.

We summarize our inferred values for H_0 and other cosmological parameters of each cosmology in Table 4. In the $\text{o}\Lambda$ CDM cosmology, both WMAP+TDSL and Planck+TDSL are consistent with a flat universe. The constraints on Ω_k from Planck+TDSL are approximately twice as large as those from Planck+BAO+JLA. In the $m_\nu\Lambda$ CDM cosmology, the upper bound of the sum of the neutrino masses Σm_ν from WMAP+TDSL is approximately twice as large as the prediction from Planck+TDSL. The addition of TDSL lowers the upper bound from Planck+BAO by about 5%. The joint constraint from Planck+BAO+TDSL yields $\Sigma m_\nu \leq 0.182$ eV with 95% probability. In the $N_{\text{eff}}\Lambda$ CDM cosmology, both WMAP+TDSL and Planck+TDSL suggest an effective number of relativistic neutrino species higher than the standard cosmological prediction of $N_{\text{eff}} = 3.046$. The Planck+TDSL value is similar in precision to Planck+BAO, yet the two values are in mild tension, the former being 1.3σ higher. The combination of Planck+BAO+TDSL yields $N_{\text{eff}} = 3.34 \pm 0.21$, also in mild tension with the standard cosmological prediction. In the w CDM cosmology, Planck+TDSL points towards $w = -1.38^{+0.14}_{-0.16}$, a result in tension with a cosmological constant ($w = -1$) at a 2.3σ level. This value is lower than other values for phantom dark energy reported in the literature (see e.g. Freedman et al. 2012; Collett & Auger 2014). With WMAP+TDSL we find $w = -1.24^{+0.16}_{-0.20}$, consistent with the previous measurement from our group using just B1608+656 and RXJ1131–1231 combined with WMAP, of ($w = -1.14^{+0.17}_{-0.20}$; Suyu et al. 2013).

5.2.2 Two-parameter extensions

We now consider cosmological models where we relax the priors on two cosmological parameters from flat Λ CDM. Following the discussion of Section 5.2.1 where we noted that the individual TDSL and Planck 95% credible regions only partially overlap, we consider here two cosmological models that reduce the tension between these two probes. First, we consider the $N_{\text{eff}}m_\nu\Lambda$ CDM model, where both the effective number of relativistic neutrino species N_{eff} as well as their total mass Σm_ν are allowed to vary. Second, we consider the ow CDM model where we relax the constraints on both the curvature, Ω_k , and the dark energy equation of state parameter w simultaneously. For the ow CDM model the Planck team does not publicly provide MCMC chains. We therefore generate additional chains using the publicly available Planck cosmological likelihood function, *plik* (Planck Collaboration et al. 2015c). Temperature power spectra were computed using the Cosmic Linear Anisotropy Solving System Boltzman code (CLASS; Blas et al. 2011; Lesgourgues & Tram 2014) and MCMC chains were generated with the MontePython sampler (Audren et al. 2013).

Figure 7 presents the two-dimensional marginalized 95% credible regions for these two models, and the bottom of Table 4 reports the 1D marginalized posterior median values and 1σ uncertainties of the corresponding

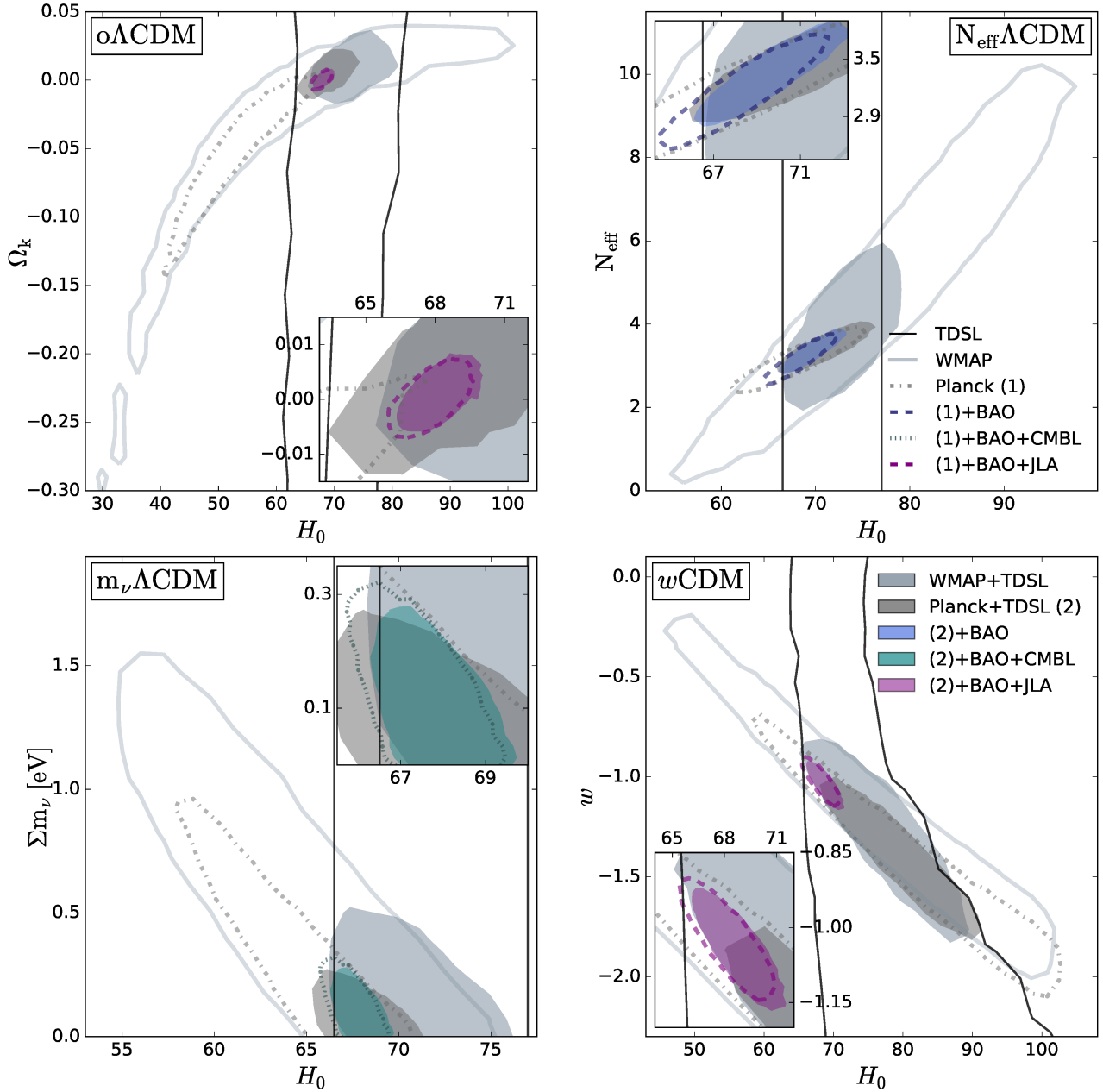


Figure 6. Cosmological constraints in one parameter extensions to Λ CDM. We consider a non-flat universe with variable curvature Ω_k (top-left), a variable effective number of relativistic neutrino species N_{eff} (top-right), a variable total mass of neutrino species Σm_ν (bottom-left, in eV) and a variable time-invariant dark energy equation of state w (bottom-right). The filled regions and colored lines delimit the marginalized 95% credible regions (consistently smoothed due to the sparsity of the samples from the available MCMC chains) with and without the constraints from TDSL respectively. The different colors represent the constraints from WMAP, Planck, Planck+CMBL, Planck+BAO, Planck+CMBL+BAO and Planck+BAO+JLA. The solid black lines delimit the 95% credible region for TDSL alone in the corresponding uniform cosmology with no additional information.

model parameters. We note that this time, the TDSL and Planck 95% credible regions are in much better agreement than in the one-parameter extension models. In the $N_{\text{eff}}m_\nu\Lambda$ CDM cosmology, Planck alone and Planck+CMBL are in agreement with the standard cosmological prediction of N_{eff} , yet the constraints are rather large. When adding TDSL, the constraints are strongly tightened and we obtain $N_{\text{eff}} = 3.44 \pm 0.24$, in mild tension with the standard cosmological prediction of $N_{\text{eff}} = 3.046$. Similarly, the constraints on the maximum neutrino mass are tight-

ened by a factor $\simeq 3$ when adding TDSL, yielding $\Sigma m_\nu \leq 0.274$ eV with 95% probability. In the $o\Lambda$ CDM cosmology, Planck+CMBL+TDSL yields $\Omega_k = -0.003^{+0.004}_{-0.004}$, in good agreement with Planck+CMBL+BAO and in favor of a flat universe. However, a tension in the dark energy equation of state w still remains, as Planck+CMBL+TDSL yields $w = -1.37^{+0.23}_{-0.18}$, 2σ lower than the cosmological constant prediction.

Table 4. Summary of the cosmological parameters constraints for the models detailed in Table 2. H_0 units are $\text{km s}^{-1} \text{Mpc}^{-1}$, Σm_ν units are eV. The quoted values are the median, 16th, and 84th percentiles, except for Σm_ν where we quote the 95% upper bound of the probability distribution. The empty slots occur when no prior samples are provided by the Planck team.

	UH_0 H_0	U Λ CDM H_0 Ω_Λ		H_0	U w CDM Ω_{de} w		H_0	Uo Λ CDM Ω_Λ Ω_k	
TDSL	$72.8^{+2.4}_{-2.4}$	$71.9^{+2.4}_{-3.0}$	$0.62^{+0.24}_{-0.35}$	$79.1^{+9.3}_{-8.7}$	$0.72^{+0.19}_{-0.34}$	$-1.79^{+0.94}_{-0.49}$	$72.5^{+2.7}_{-3.0}$	$0.51^{+0.28}_{-0.30}$	$0.1^{+0.3}_{-0.3}$

	H_0	o Λ CDM Ω_m Ω_Λ Ω_k			H_0	w CDM Ω_{de} w	
TDSL+WMAP	$73.0^{+2.3}_{-2.5}$	$0.25^{+0.02}_{-0.02}$	$0.74^{+0.02}_{-0.02}$	$0.005^{+0.005}_{-0.005}$	$76.5^{+4.6}_{-3.9}$	$0.76^{+0.02}_{-0.02}$	$-1.24^{+0.16}_{-0.20}$
TDSL+Planck (1)	$69.2^{+1.4}_{-2.2}$	$0.30^{+0.02}_{-0.02}$	$0.70^{+0.01}_{-0.01}$	$0.003^{+0.004}_{-0.006}$	$79.0^{+4.4}_{-4.2}$	$0.77^{+0.02}_{-0.03}$	$-1.38^{+0.14}_{-0.16}$
(1)+BAO	$68.0^{+0.7}_{-0.7}$	$0.31^{+0.01}_{-0.01}$	$0.69^{+0.01}_{-0.01}$	$0.001^{+0.003}_{-0.003}$	$69.6^{+1.8}_{-1.7}$	$0.70^{+0.01}_{-0.01}$	$-1.08^{+0.07}_{-0.08}$
(1)+BAO+JLA	$68.1^{+0.7}_{-0.7}$	$0.31^{+0.01}_{-0.01}$	$0.69^{+0.01}_{-0.01}$	$0.001^{+0.003}_{-0.003}$	$68.8^{+1.0}_{-1.0}$	$0.70^{+0.01}_{-0.01}$	$-1.04^{+0.05}_{-0.05}$

	H_0	$N_{\text{eff}}\Lambda$ CDM Ω_Λ N_{eff}		H_0	$m_\nu\Lambda$ CDM Ω_Λ Σm_ν (eV)	
TDSL+WMAP	$73.2^{+2.2}_{-2.4}$	$0.72^{+0.02}_{-0.03}$	$3.86^{+0.73}_{-0.71}$	$70.7^{+1.9}_{-1.9}$	$0.73^{+0.02}_{-0.02}$	≤ 0.393
TDSL+Planck (1)	$71.0^{+2.0}_{-2.0}$	$0.71^{+0.01}_{-0.01}$	$3.45^{+0.23}_{-0.24}$	$68.1^{+1.1}_{-1.2}$	$0.70^{+0.01}_{-0.02}$	≤ 0.199
(1)+BAO	$69.6^{+1.4}_{-1.3}$	$0.70^{+0.01}_{-0.01}$	$3.34^{+0.21}_{-0.21}$	$67.9^{+0.6}_{-0.6}$	$0.69^{+0.01}_{-0.01}$	≤ 0.182
(1)+BAO+CMBL				$67.9^{+0.6}_{-0.7}$	$0.69^{+0.01}_{-0.01}$	≤ 0.216

	H_0	$N_{\text{eff}}m_\nu\Lambda$ CDM Ω_Λ N_{eff} Σm_ν (eV)			H_0	o w CDM Ω_{de} Ω_k w		
TDSL+Planck (1)	$70.8^{+2.0}_{-2.1}$	$0.71^{+0.02}_{-0.02}$	$3.44^{+0.24}_{-0.24}$	≤ 0.274	$88.4^{+5.9}_{-7.2}$	$0.83^{+0.02}_{-0.03}$	$-0.010^{+0.003}_{-0.003}$	$-2.10^{+0.34}_{-0.41}$
(1)+CMBL	$70.8^{+2.1}_{-2.1}$	$0.71^{+0.02}_{-0.02}$	$3.44^{+0.25}_{-0.24}$	≤ 0.347	$77.9^{+5.0}_{-4.2}$	$0.77^{+0.03}_{-0.03}$	$-0.003^{+0.004}_{-0.004}$	$-1.37^{+0.18}_{-0.23}$
(1)+BAO+CMBL					$70.0^{+2.1}_{-1.7}$	$0.71^{+0.02}_{-0.02}$	$-0.000^{+0.004}_{-0.003}$	$-1.07^{+0.09}_{-0.10}$

6 CONCLUSIONS

Using multiple telescopes in the Southern and Northern hemispheres, we have monitored the quadruple imaged strong gravitational lens HE 0435–1223 for 13 years with an average cadence of one observing epoch every 3.6 days. We analyse the imaging data using the MCS deconvolution algorithm (Magain et al. 1998) on a total of 876 observing epochs to produce the light curves of the four lensed images, with an rms photometric precision of 10 mmag on the brightest quasar image.

We measured the time delays between each pair of lensed images using the free-knot spline technique and the regression difference technique from the PyCS package (Tewes et al. 2013a). Our uncertainty estimation involves the generation of synthetic light curves that closely mimic the intrinsic and extrinsic features of the real data. To test the robustness of our measurements, we vary parameters such as the number of knots in the splines, the initial parameters used for the deconvolution photometry, and the length of the considered light curves. The two curve shifting techniques agree well with each other both on the point estimation of the delays and on the estimated uncertainty. The smallest relative uncertainty, of 6.5%, is obtained for

the A-D pair of images. For this pair involving image A, our present measurement is twice as precise as the earlier result by Courbin et al. (2011).

In H0LiCOW Paper IV, we use our new COSMOGRAIL time delays for HE 0435–1223 to compute its time-delay distance. Very importantly, this is done in a blind way with respect to the inference of cosmological parameters. In this paper, we combine the time-delay distance likelihoods from HE 0435–1223 with the published ones from B1608+656 and RXJ1131–1231 to create a Time Delays Strong Lensing (TDSL) probe. We also combine the latter with other cosmological probes such as WMAP, Planck, BAO and JLA to constrain cosmological parameters for a large range of extended cosmological models. Our main conclusions are as follows:

- TDSL alone is weakly sensitive to the matter density, Ω_m , curvature, Ω_k and dark energy density Ω_{de} and equation of state w . Its primary sensitivity to H_0 allows us to break degeneracies of CMB probes in extended cosmological models.
- In a flat Λ CDM cosmology with uniform priors on H_0 and Ω_m , TDSL alone yields $H_0 = 71.9^{+2.4}_{-3.0} \text{ km s}^{-1} \text{ Mpc}^{-1}$. When enforcing $\Omega_m=0.32$ from the most recent Planck re-

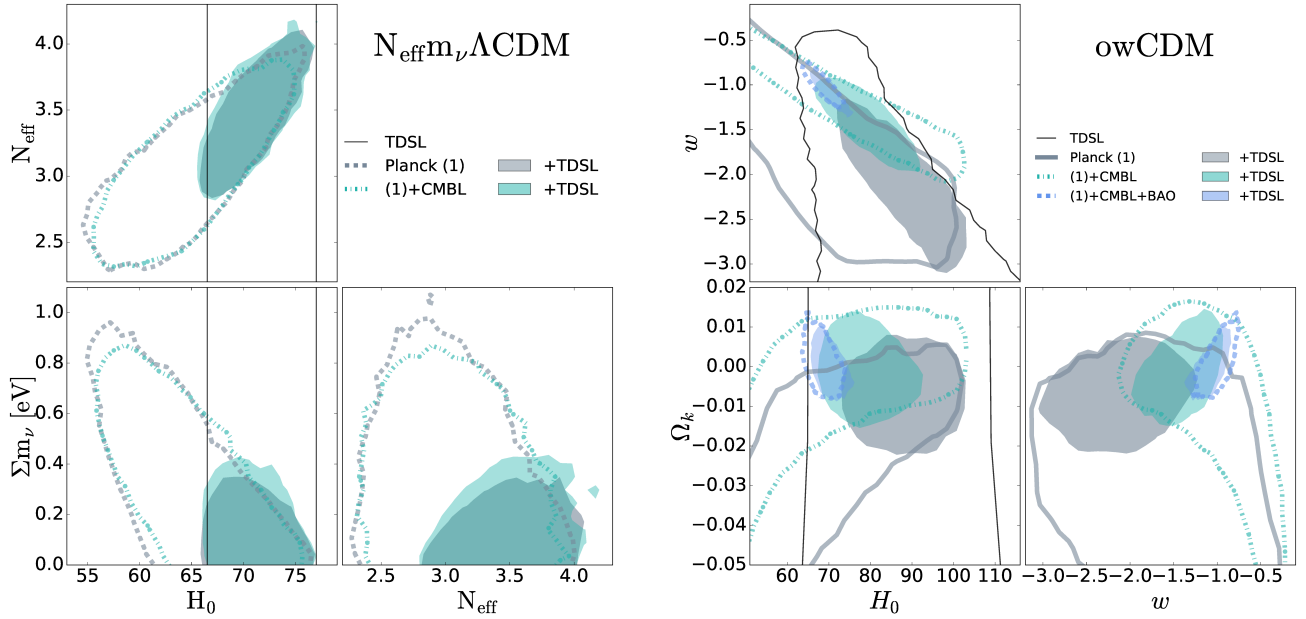


Figure 7. Cosmological constraints in two-parameter extensions to Λ CDM. We consider a flat Universe with variable effective number of relativistic neutrino species N_{eff} and total mass of neutrinos Σm_ν (left), and an open universe with variable dark energy equation of state parameters w (right). The colored lines and filled areas are the same as in Figure 6, and show marginalized 95% credible regions. The TDSL contours in the ow CDM cosmology are computed using uniform priors on Ω_k $[-0.5, 0.5]$ and w $[-2.5, 0.5]$.

sults, we find $H_0 = 72.8 \pm 2.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$. These results are in excellent agreement with the most recent measurements using the distance ladder, but are in tension with the CMB measurements from Planck.

- In a non-flat Λ CDM cosmology, we find, using TDSL and Planck, $H_0 = 69.2^{+1.4}_{-2.2} \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $\Omega_k = 0.003^{+0.004}_{-0.006}$, in agreement with a flat universe.

- In a flat w CDM cosmology in combination with Planck, we find a 2.3σ tension from a cosmological constant in favor of a phantom form of dark energy. Our joint constraints in this cosmology are $H_0 = 79.0^{+4.4}_{-4.2} \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_{\text{de}} = 0.77^{+0.02}_{-0.03}$ and $w = -1.38^{+0.14}_{-0.16}$.

- In a flat $m_\nu \Lambda$ CDM cosmology, in combination with Planck and BAO we tighten the constraints on the maximum mass of neutrinos to $\Sigma m_\nu \leq 0.182 \text{ eV}$, while removing the tension in H_0 .

- In a flat $N_{\text{eff}} \Lambda$ CDM cosmology, in combination with Planck and BAO we find $N_{\text{eff}} = 3.34 \pm 0.21$, i.e. 1.3σ higher than the standard cosmological value. This mild tension remains when the constraints on both Σm_ν and N_{eff} are relaxed.

- In a ow CDM cosmology, in combination with Planck and CMBL, we find $H_0 = 77.9^{+5.0}_{-4.2} \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_{\text{de}} = 0.77^{+0.03}_{-0.03}$, $\Omega_k = -0.003^{+0.004}_{-0.004}$ and $w = -1.37^{+0.18}_{-0.23}$. Similarly to the $o\Lambda$ CDM and w CDM cosmologies, we are in good agreement with a flat universe and in tension with a cosmological constant, respectively.

The combined strengths of our H0LiCOW lens modeling and COSMOGRAIL monitoring indicate that quasar time-delay cosmography is now a mature field, producing precise and accurate inferences of cosmological parameters, that are independent of any other cosmological probe. Still, our results can be improved in at least five ways:

(i) Continuing to enlarge the sample. Two more objects with excellent time-delay measurements as well as high-resolution imaging and spectroscopic data remain to be analysed in the H0LiCOW project (see H0LiCOW Paper I). When completed, H0LiCOW is expected to provide a measurement of H_0 to better than 3.5% in a non-flat Λ CDM universe with flat priors on Ω_m and Ω_Λ . Data of quality comparable to those obtained for H0LiCOW are in the process of being obtained for another four systems with measured time delays from COSMOGRAIL (HST-GO-14254; PI: Treu). Meanwhile, current and planned wide field imaging surveys such as DES, KiDS, HSC, LSST, Euclid and WFIRST, should discover hundreds of new gravitational lens systems suitable for time-delay cosmography (Oguri & Marshall 2010). For example, the dedicated search in the Dark Energy Survey STRIDES⁷ has already confirmed two new lenses from the Year1 data (Agnello et al. 2016).

(ii) Improve the lens modeling accuracy. The tests carried out in our current (H0LiCOW Paper IV) and past work (Suyu et al. 2014), the good internal agreement between the three measured systems (Section 5.1), and independent analysis based on completely independent codes (Birrer et al. 2015), show that our lens models are sufficiently complex given the currently available data. However, as the number of systems being analysed grows, random uncertainties in the cosmological parameters will fall, and residual systematic uncertainties related to degeneracies inherent to gravitational lensing will need to be investigated in more detail. Following the work of Xu et al. (2016), detailed hydro N-body simulations of lensing galaxies in combination with ray-shooting can be used to evaluate the impact of the lensing degeneracies on cosmological results in view of future

⁷ strides.astro.ucla.edu

observations with the JWST or 30-m class ground-based telescopes with adaptive optics, and to drive development of improved lens modeling techniques and assumptions appropriate to the density structures we expect.

(iii) Improve the absolute mass calibration. Spatially resolved 2D kinematics of the lens galaxies, to be obtained either with JWST and with integral field spectrographs mounted on large ground-based telescopes with adaptive optics, should further improve both the precision for each system and our ability to test for residual systematics, including those arising from the mass sheet and source position transformations (Schneider & Sluse 2013, 2014; Unruh et al. 2016). The same data should also allow us to use constraints from the stellar mass or mass profile of lens galaxies as attempted in Courbin et al. (2011) with slit spectroscopy.

(iv) Measuring time delays with the current photometric precision and time sampling of monitoring data requires long and time-consuming campaigns, and is currently not possible for hundreds of objects. Increasing the monitoring efficiency is possible, by catching extremely small (mmag) and fast (days) variations in the quasar light curves. Such data can be obtained with daily observations with 2-m class telescopes in good seeing conditions, a project that will be implemented in the context of the extended COSMOGRAIL program (eCOSMOGRAIL; Courbin et al. 2016, in prep) to measure quasar time delays in only 1 or 2 observing seasons. Furthermore, in the long run, LSST should be able to provide sufficiently accurate time delays for hundreds of systems from the survey data itself (Liao et al. 2015), and enable sub-percent precision on H_0 in the next decade (Treu & Marshall 2016).

ACKNOWLEDGMENTS

We thank Adriano Agnello, Roger Blandford, Geoff ChihFan Chen, Xuheng Ding, Yashar Hezaveh, Kai Liao, John McKean, Danka Paraficz, Olga Tihhonova, and Simona Vegetti for their contributions to the H0LiCOW project. We thank all the observers at the Euler, SMARTS, Mercator and Maidanak telescopes who participated in the queue-mode observations. H0LiCOW and COSMOGRAIL are made possible thanks to the continuous work of all observers and technical staff obtaining the monitoring observations, in particular at the Swiss Euler telescope at La Silla Observatory. The Euler telescope is supported by the Swiss National Science Foundation. We are grateful to Thomas Tram for expert help in implementing CLASS and MontePython to create MCMC chains for non-standard cosmologies. Numerical computations for the CMB likelihoods were done on the Sciamia High Performance Compute (HPC) cluster which is supported by the ICG, SEPNet and the University of Portsmouth V.B., F.C. and G.M. acknowledge the support of the Swiss National Science Foundation (SNSF). S.H.S. acknowledges support from the Max Planck Society through the Max Planck Research Group. This work is supported in part by the Ministry of Science and Technology in Taiwan via grant MOST-103-2112-M-001-003-MY3. K.C.W. is supported by an EACOA Fellowship awarded by the East Asia Core Observatories Association, which consists of the Academia Sinica Institute of Astronomy and Astrophysics, the National Astronomical Observatory of

Japan, the National Astronomical Observatories of the Chinese Academy of Sciences, and the Korea Astronomy and Space Science Institute. P.J.M. acknowledges support from the U.S. Department of Energy under contract number DE-AC02-76SF00515. C.E.R. and C.D.F. were funded through the NSF grant AST-1312329, ‘‘Collaborative Research: Accurate cosmology with strong gravitational lens time delays,’’ and the *HST* grant GO-12889. D.S. acknowledges funding support from a *Back to Belgium* grant from the Belgian Federal Science Policy (BELSPO). M.T. acknowledges support by a fellowship of the Alexander von Humboldt Foundation and the DFG grant Hi 1495/2-1. S.H. acknowledges support by the DFG cluster of excellence ‘‘Origin and Structure of the Universe’’ (www.universe-cluster.de). T.T. thanks the Packard Foundation for generous support through a Packard Research Fellowship, the NSF for funding through NSF grant AST-1450141, ‘‘Collaborative Research: Accurate cosmology with strong gravitational lens time delays’’. L.V.E.K. is supported in part through an NWO-VICI career grant (project number 639.043.308).

Based on observations made with the NASA/ESA Hubble Space Telescope, obtained at the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS 5-26555. These observations are associated with program #12889, #10158, #9744 and #7422. Support for program #12889 was provided by NASA through a grant from the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS 5-26555.

REFERENCES

- Addison G. E., Huang Y., Watts D. J., Bennett C. L., Halpern M., Hinshaw G., Weiland J. L., 2016, *ApJ*, **818**, 132
- Agnello A., Sonnenfeld A., Suyu S. H., Treu T., Fassnacht C. D., Mason C., Bradač M., Auger M. W., 2016, *MNRAS*, **458**, 3830
- Anderson L., et al., 2012, *MNRAS*, **427**, 3435
- Audren B., Lesgourgues J., Benabed K., Prunet S., 2013, *J. Cosmology Astropart. Phys.*, **2**, 001
- Bennett C. L., et al., 2013, *ApJS*, **208**, 20
- Bertin E., Arnouts S., 1996, *A&AS*, **117**, 393
- Betoule M., et al., 2013, *A&A*, **552**, A124
- Beutler F., et al., 2011, *MNRAS*, **416**, 3017
- Birrer S., Amara A., Refregier A., 2015, preprint, ([arXiv:1511.03662](https://arxiv.org/abs/1511.03662))
- Blackburne J. A., Kochanek C. S., Chen B., Dai X., Chartas G., 2014, *ApJ*, **789**, 125
- Blake C., et al., 2011, *MNRAS*, **418**, 1707
- Blas D., Lesgourgues J., Tram T., 2011, CLASS: Cosmic Linear Anisotropy Solving System, Astrophysics Source Code Library (ascl:1106.020)
- Bonamente M., Joy M. K., LaRoque S. J., Carlstrom J. E., Reese E. D., Dawson K. S., 2006, *ApJ*, **647**, 25
- Bonvin V., Tewes M., Courbin F., Kuntzer T., Sluse D., Meylan G., 2016, *Astronomy and Astrophysics*, **585**, A88
- Braibant L., Hutsemékers D., Sluse D., Anguita T., García-Vergara C. J., 2014, *A&A*, **565**, L11
- Cantale N., Courbin F., Tewes M., Jablonka. P., Meylan G., 2016, [ArXiv1602.02167](https://arxiv.org/abs/1602.02167),
- Chen G. C. F., et al., 2016, [ArXiv1601.01321](https://arxiv.org/abs/1601.01321),
- Collett T. E., Auger M. W., 2014, *MNRAS*, **443**, 969
- Collett T. E., et al., 2013, *MNRAS*, **432**, 679

- Courbin F., Eigenbrod A., Vuissoz C., Meylan G., Magain P., 2005, in Mellier Y., Meylan G., eds, IAU Symposium Vol. 225, Gravitational Lensing Impact on Cosmology. pp 297–303, doi:10.1017/S1743921305002097
- Courbin F., et al., 2011, *Astronomy and Astrophysics*, **536**, A53
- Di Valentino E., Melchiorri A., Silk J., 2016, ArXiv1606.00634,
- Dobler G., Fassnacht C. D., Treu T., Marshall P., Liao K., Hojjati A., Linder E., Rumbaugh N., 2015, *ApJ*, **799**, 168
- Efstathiou G., 2014, *MNRAS*, **440**, 1138
- Eigenbrod A., Courbin F., Dye S., Meylan G., Sluse D., Vuissoz C., Magain P., 2006a, *A&A*, **451**, 747
- Eigenbrod A., Courbin F., Meylan G., Vuissoz C., Magain P., 2006b, *A&A*, **451**, 759
- Eulaers E., et al., 2013, *A&A*, **553**, A121
- Falco E. E., Gorenstein M. V., Shapiro I. I., 1985, *ApJ*, **289**, L1
- Fassnacht C. D., Xanthopoulos E., Koopmans L. V. E., Rusin D., 2002, *ApJ*, **581**, 823
- Fassnacht C. D., Gal R. R., Lubin L. M., McKean J. P., Squires G. K., Readhead A. C. S., 2006, *ApJ*, **642**, 30
- Fassnacht C. D., Koopmans L. V. E., Wong K. C., 2011, *MNRAS*, **410**, 2167
- Freedman W. L., Madore B. F., Scowcroft V., Burns C., Monson A., Persson S. E., Seibert M., Rigby J., 2012, *ApJ*, **758**, 24
- Gao F., et al., 2016, *ApJ*, **817**, 128
- Giusarma E., Gerbino M., Mena O., Vagnozzi S., Ho S., Freese K., 2016, ArXiv1605.04320,
- Greene Z. S., et al., 2013, *ApJ*, **768**, 39
- Heavens A., Jimenez R., Verde L., 2014, *Physical Review Letters*, **113**, 241302
- Heymans C., et al., 2012, *MNRAS*, **427**, 146
- Hilbert S., White S. D. M., Hartlap J., Schneider P., 2007, *MNRAS*, **382**, 121
- Hilbert S., Hartlap J., White S. D. M., Schneider P., 2009, *A&A*, **499**, 31
- Hinshaw G., et al., 2013, *ApJS*, **208**, 19
- Kochanek C. S., 2002, *ApJ*, **578**, 25
- Kochanek C. S., Morgan N. D., Falco E. E., McLeod B. A., Winn J. N., Dembicky J., Ketzeback B., 2006, *ApJ*, **640**, 47
- Lesgourgues J., Tram T., 2014, *J. Cosmology Astropart. Phys.*, **9**, 032
- Lewis A., Bridle S., 2002, *Phys. Rev. D*, **66**, 103511
- Liao K., et al., 2015, *ApJ*, **800**, 11
- Linder E. V., 2011, *Phys. Rev. D*, **84**, 123529
- Magain P., Courbin F., Sohy S., 1998, *ApJ*, **494**, 472
- Marshall P., Rajguru N., Slosar A., 2006, *Phys. Rev. D*, **73**, 067302
- McCully C., Keeton C. R., Wong K. C., Zabludoff A. I., 2014, *MNRAS*, **443**, 3631
- McCully C., Keeton C. R., Wong K. C., Zabludoff A. I., 2016, ArXiv1601.05417,
- Molinari N., Durand J., Sabatier R., 2004, *Computational Statistics & Data Analysis*, **45**, 159
- Momcheva I. G., Williams K. A., Cool R. J., Keeton C. R., Zabludoff A. I., 2015, *ApJS*, **219**, 29
- Morgan N. D., Kochanek C. S., Pevunova O., Schechter P. L., 2005, *AJ*, **129**, 2531
- Oguri M., Marshall P. J., 2010, *MNRAS*, **405**, 2579
- Padmanabhan N., Xu X., Eisenstein D. J., Scalzo R., Cuesta A. J., Mehta K. T., Kazin E., 2012, *MNRAS*, **427**, 2132
- Pelt J., Kayser R., Refsdal S., Schramm T., 1996, *A&A*, **305**, 97
- Percival W. J., et al., 2010, *MNRAS*, **401**, 2148
- Planck Collaboration et al., 2014, *A&A*, **571**, A16
- Planck Collaboration et al., 2015a, ArXiv1502.01589,
- Planck Collaboration et al., 2015b, ArXiv1502.01591,
- Planck Collaboration et al., 2015c, preprint, (arXiv:1502.01593)
- Rathna Kumar S., et al., 2013, *A&A*, **557**, A44
- Refsdal S., 1964, *MNRAS*, **128**, 307
- Riess A. G., et al., 2016, ArXiv1604.01424,
- Rigault M., et al., 2015, *ApJ*, **802**, 20
- Salvatelli V., Marchini A., Lopez-Honorez L., Mena O., 2013, *Phys. Rev. D*, **88**, 023531
- Schneider P., Sluse D., 2013, *A&A*, **559**, A37
- Schneider P., Sluse D., 2014, *A&A*, **564**, A103
- Sluse D., Tewes M., 2014, *A&A*, **571**, A60
- Sluse D., Hutsemékers D., Courbin F., Meylan G., Wambsgans J., 2012, *A&A*, **544**, A62
- Sorce J. G., Tully R. B., Courtois H. M., 2012, *ApJ*, **758**, L12
- Spergel D. N., Flauger R., Hložek R., 2015, *Phys. Rev. D*, **91**, 023518
- Suyu S. H., Halkola A., 2010, *A&A*, **524**, A94
- Suyu S. H., Marshall P. J., Hobson M. P., Blandford R. D., 2006, *MNRAS*, **371**, 983
- Suyu S. H., Marshall P. J., Auger M. W., Hilbert S., Blandford R. D., Koopmans L. V. E., Fassnacht C. D., Treu T., 2010, *ApJ*, **711**, 201
- Suyu S. H., et al., 2012, *ApJ*, **750**, 10
- Suyu S. H., et al., 2013, *ApJ*, **766**, 70
- Suyu S. H., et al., 2014, *ApJ*, **788**, L35
- Tewes M., Courbin F., Meylan G., 2013a, *A&A*, **553**, A120
- Tewes M., et al., 2013b, *A&A*, **556**, A22
- Treu T., 2010, *ARA&A*, **48**, 87
- Treu T., Marshall P. J., 2016, *A&ARv*, in press,
- Unruh S., Schneider P., Sluse D., 2016, ArXiv1606.04321,
- Weinberg D. H., Mortonson M. J., Eisenstein D. J., Hirata C., Riess A. G., Rozo E., 2013, *Phys. Rep.*, **530**, 87
- Wisotzki L., Christlieb N., Bade N., Beckmann V., Köhler T., Vanelle C., Reimers D., 2000, *A&A*, **358**, 77
- Wisotzki L., Schechter P. L., Bradt H. V., Heinmüller J., Reimers D., 2002, *A&A*, **395**, 17
- Wong K. C., Keeton C. R., Williams K. A., Momcheva I. G., Zabludoff A. I., 2011, *ApJ*, **726**, 84
- Wucknitz O., 2002, *MNRAS*, **332**, 951
- Xu D., Sluse D., Schneider P., Springel V., Vogelsberger M., Nelson D., Hernquist L., 2016, *MNRAS*, **456**, 739